

Visual perception

Visualizzazione dell'Informazione Quantitativa

<http://softeng.polito.it/courses/VIQ>



SoftEng
<http://softeng.polito.it>

Version 1.6.0
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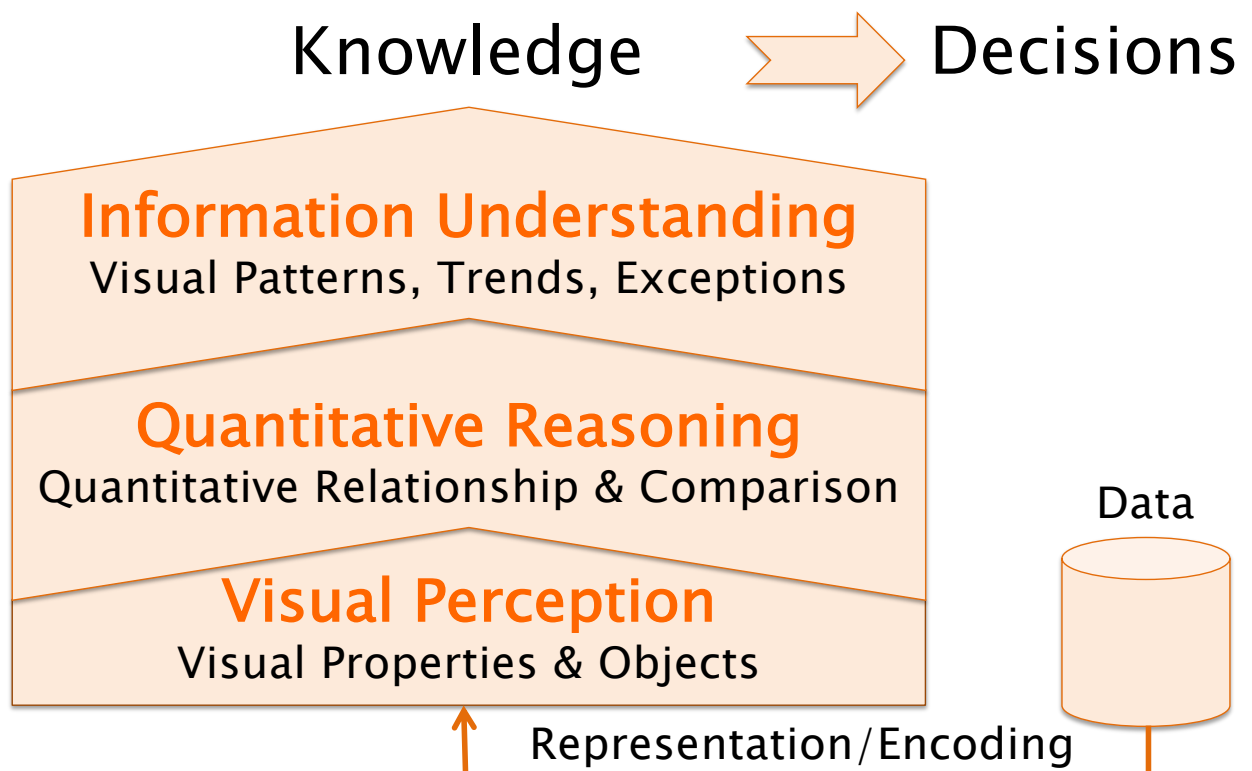
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VISUALIZATION PIPELINE

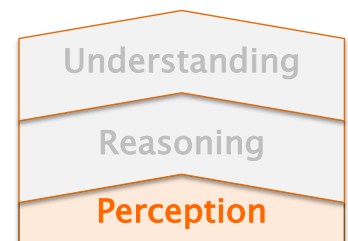
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Visualization Pipeline



Visual Perception

- Any variable (measure) must be **visually encoded**, i.e. we need to identify:
 - ♦ Visual object to represent entity
 - ♦ Visual attribute to represent the measure



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Example

Votes received by four candidates in recent elections

Candidate	Votes	Proportion
Sergio	197800	50.09%
Alberto	140545	35.59%
Giorgio	53748	13.61%
Valter	2759	0.70%

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Encoding

- Visual object: line
- Visual attribute: length

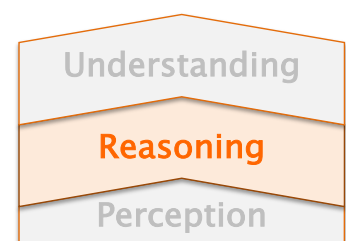


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Visual Reasoning

Layout and visual attributes allow:

- **Discrimination**
 - ◆ Distinguish visual objects or group of –
- **Comparison**
 - ◆ Place visual objects in order
- **Magnitude assessment**
 - ◆ Evaluate the (relative) magnitude of visual objects



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Reasoning

Alberto

- Giorgio
Valter

Sergio

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Reasoning

- Discrimination

Alberto

Valter -

Giorgio

Sergio

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Reasoning

- Comparison



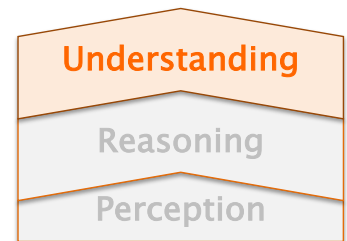
Reasoning

- Assessment



Understanding

- Variation within quantitative measures
 - ◆ Distribution
 - ◆ Deviation
 - ◆ Correlation
- Variation within category
 - ◆ Ranking
 - ◆ Part-to-whole
 - ◆ Time
 - ◆ Space
- Multivariate



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Understanding



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Understanding

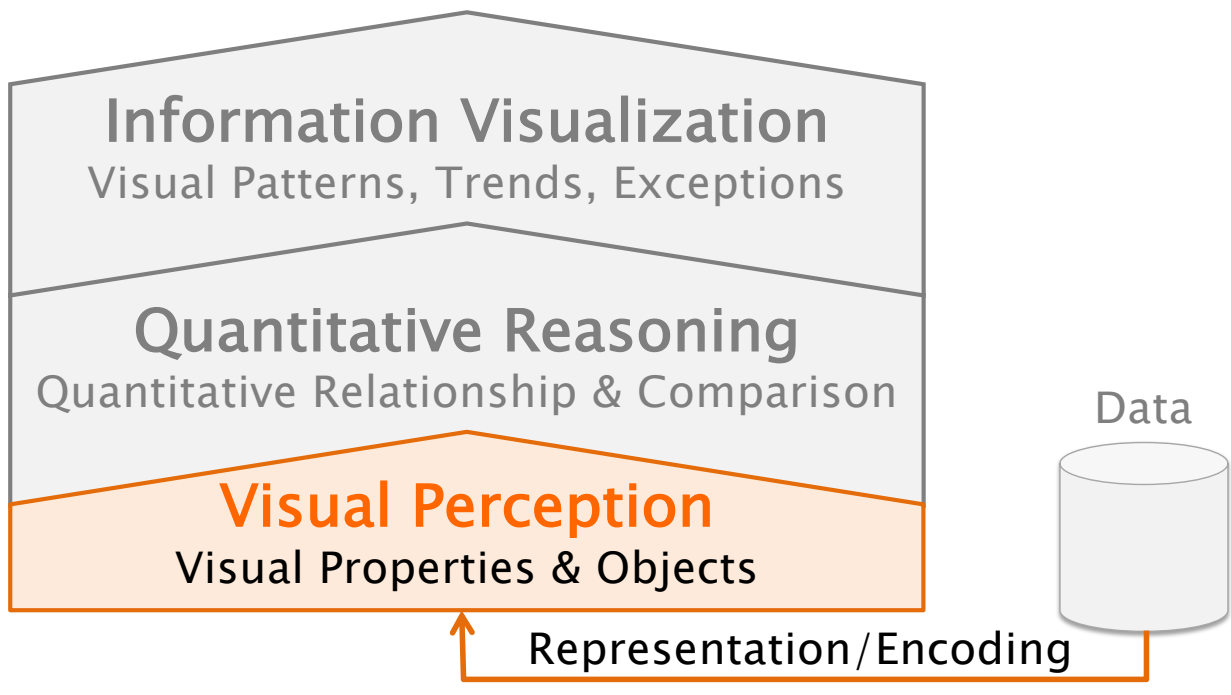
- Ranking



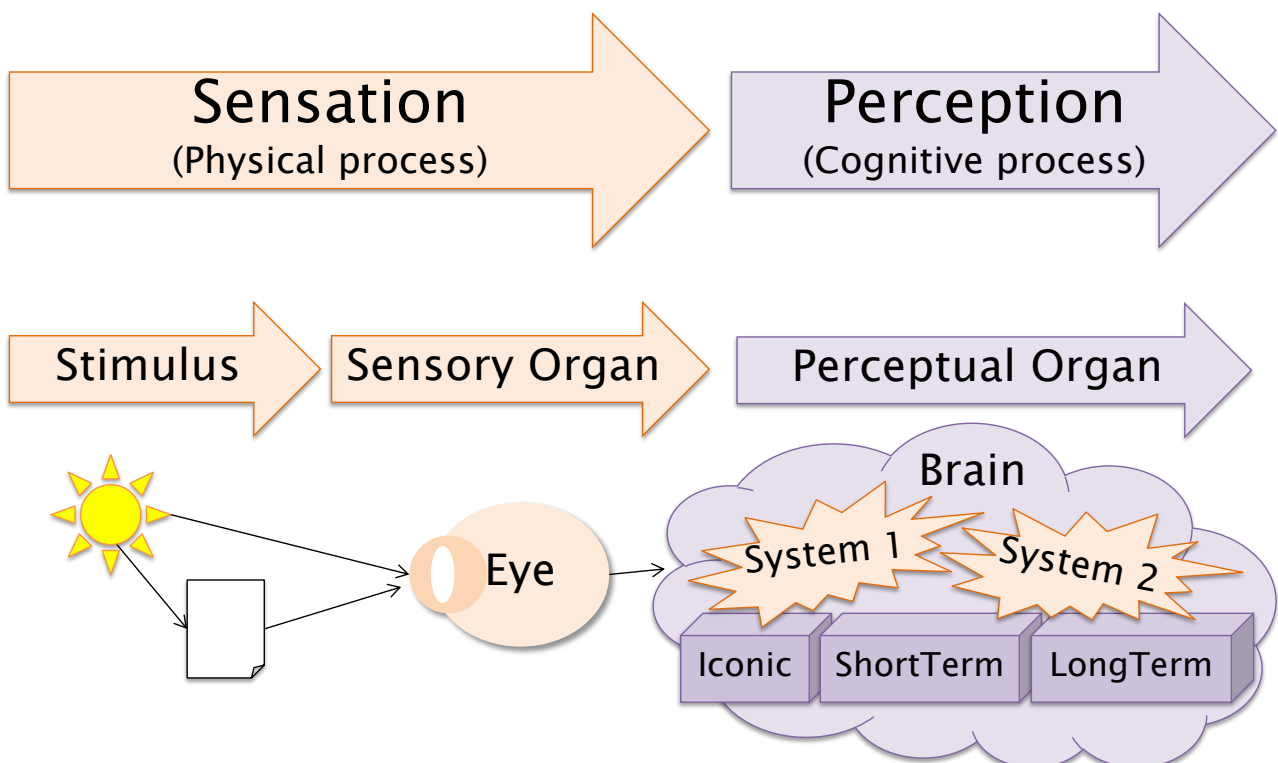
VISUAL PERCEPTION

Data Visualization

Understanding



Visual perception



Memory Hierarchy

- Iconic memory (visual sensory register)
 - ♦ Pre-attentive processing
 - ♦ Detects a **limited number of attributes**
- Short-term memory (working memory)
 - ♦ Store visual chunks
 - ♦ Limited number
- Long-term memory
 - ♦ Store high-level knowledge

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Simplified Model

- The three levels of memory represent a simplified model
 - ♦ does not correspond to “real” physical structure
- Useful to explain a few phenomena
 - ♦ The 7 ± 2 rule
 - ♦ Change blindness

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Change blindness



<http://www2.psych.ubc.ca/~rensink/flicker/download/index.html>

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Pre-Attentive Attributes

5 7 8 4 9 8 3 1 1 0 6 8 8 2 1 1 5 2 6 6 5
9 5 1 8 4 6 8 4 9 3 0 4 5 3 4 9 2 5 8 5 8
5 0 5 4 6 2 6 5 7 3 7 8 6 5 3 7 2 6 3 1 5
5 8 6 6 8 3 7 6 5 0 9 6 3 4 6 1 9 5 6 6 4
1 6 7 3 9 9 2 8 3 4 0 3 5 1 6 3 5 3 9 3 4
8 6 9 7 5 4 2 4 7 4 9 5 8 5 3 0 7 6 0 6 7
0 3 1 5 3 2 3 5 6 7 2 8 9 8 5 3 7 8 8 2 4
5 5 3 4 8 1 5 6 2 3 5 5 1 2 1 0 8 7 2 6 3
7 4 3 8 4 8 2 6 7 9 5 6 2 3 6 7 8 0 8 3 6
4 9 5 6 7 2 2 2 8 3 1 1 0 1 8 6 2 6 2 1 4

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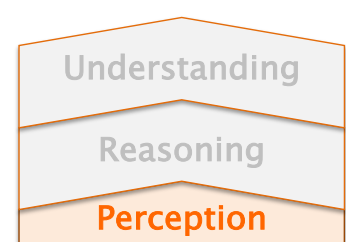
Pre-Attentive Attributes

5 7 8 4 9 8 3 1 1 0 6 8 8 2 1 1 5 2 6 6 5
9 5 1 8 4 6 8 4 9 3 0 4 5 3 4 9 2 5 8 5 8
5 0 5 4 6 2 6 5 7 3 7 8 6 5 3 7 2 6 3 1 5
5 8 6 6 8 3 7 6 5 0 9 6 3 4 6 1 9 5 6 6 4
1 6 7 3 9 9 2 8 3 4 0 3 5 1 6 3 5 3 9 3 4
8 6 9 7 5 4 2 4 7 4 9 5 8 5 3 0 7 6 0 6 7
0 3 1 5 3 2 3 5 6 7 2 8 9 8 5 3 7 8 8 2 4
5 5 3 4 8 1 5 6 2 3 5 5 1 2 1 0 8 7 2 6 3
7 4 3 8 4 8 2 6 7 9 5 6 2 3 6 7 8 0 8 3 6
4 9 5 6 7 2 2 2 8 3 1 1 0 1 8 6 2 6 2 1 4

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Encoding

- Encoding is the key to enable visual perception
 - ◆ Visual object to represent entity
 - ◆ Visual attribute to represent the measure
- Two main types
 - ◆ Quantitative (different properties)
 - ◆ Categorical (ordinal or not)



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Pre-Attentive attributes

Category	Attribute
Form	Orientation Length/distance Line width Size Shape Curvature Added marks Enclosure
Color	Hue Intensity
Spatial position	2-D position
Motion	Flicker Direction Speed

Perception task

Visual attributes allow:

- Discrimination
 - ◆ Distinguish visual objects
- Comparison
 - ◆ Place visual objects in order
- Magnitude assessment
 - ◆ Evaluate the (relative) magnitude of visual objects

Just noticeable difference

- Given a physical dimension (length, brightness, etc.) x
- d is the **just noticeable difference** if:
 - ♦ difference between x and $x+d$ is perceivable
 - ♦ but not smaller differences
- d depends on many factors:
 - ♦ Subject
 - ♦ Environment
 - ♦ Physical dimension

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Weber's law

- Just noticeable difference d is:

$$d_p(x) = k_p \cdot x$$

- Where
 - ♦ x : dimension
 - ♦ $d_p(x)$: just noticeable difference
 - ♦ k_p : constant
 - Subjective
 - Environmental

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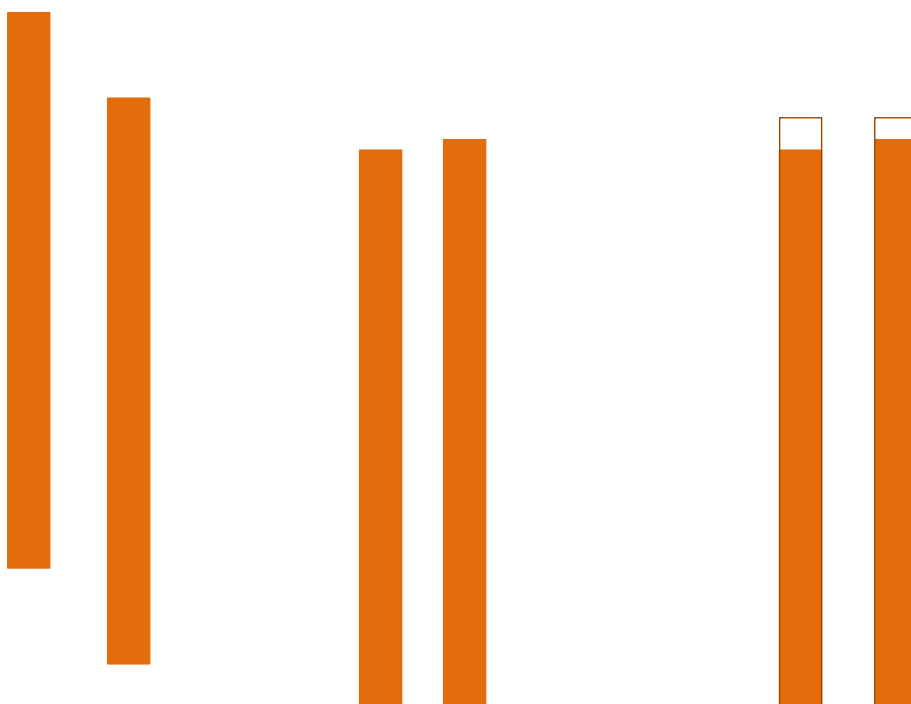
Consequences of Weber's law

- It is easier to compare lengths that differ by a large percentage
- The same difference is easier to notice between smaller measures
 - ♦ More likely to be larger than just noticeable difference

$$x < y \implies d_p(x) < d_p(y)$$

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Non-aligned objects lengths



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Non-aligned objects lengths

- Additional references may help comparison
 - ♦ They provide alternative possible comparisons
- If lengths range between 0 and a maximum (L), e.g. percentages
- Comparing l_1 and l_2 (close to L) that differ by a small amount d
 - ♦ Difference $L-l_1$ vs. $L-l_2$ easier to notice than l_1 vs. l_2

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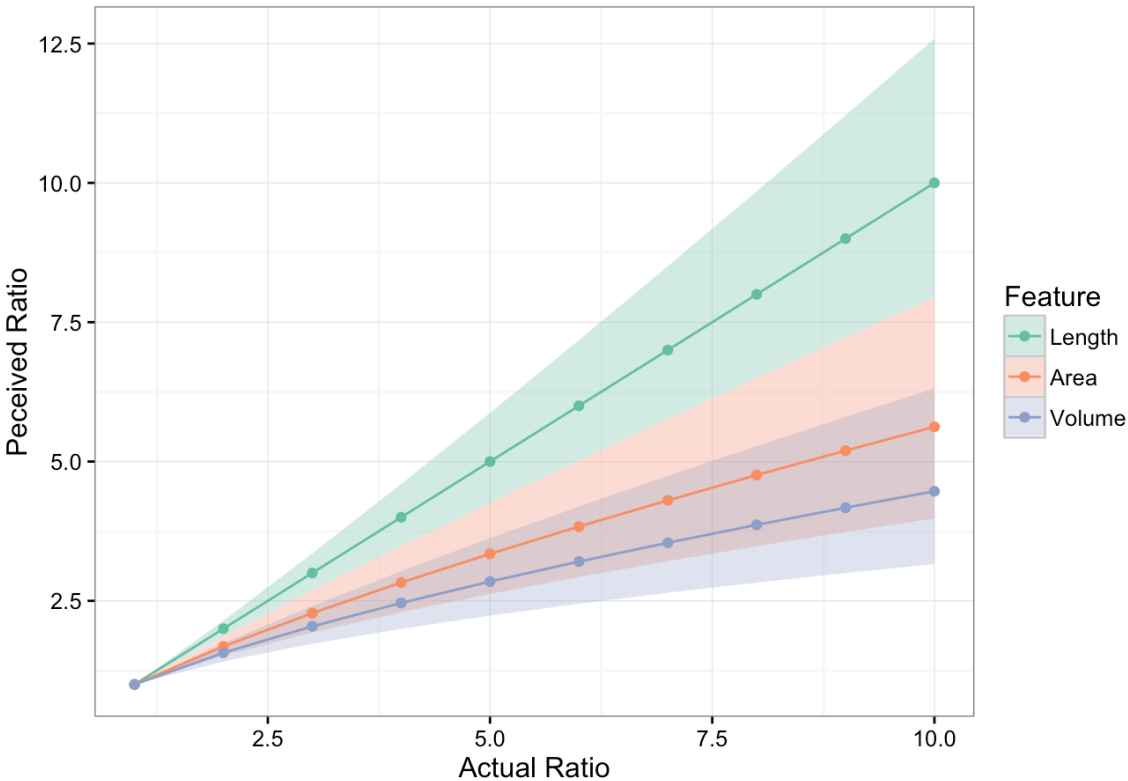
Stevens's law

- Perceive scale (magnitude ratio)

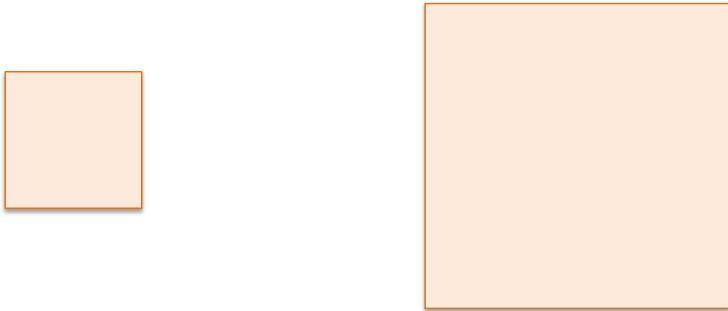
$$p(x) = c \cdot x^\beta$$

- Where β depends on spatial dimension
 - ♦ 1D: Length $\rightarrow \beta$ in [0.9, 1.1]
 - ♦ 2D: Area $\rightarrow \beta$ in [0.6, 0.9]
 - ♦ 3D: Volume $\rightarrow \beta$ in [0.5, 0.8]

Steven's law



Steven's law



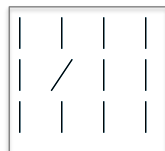
Consequences

- Prefer comparing lengths
- Avoid comparison between areas
 - ♦ Except for ordinal measures
- Never–ever make volume comparisons

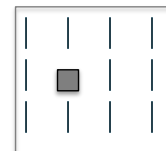
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Attributes of form

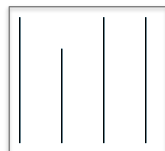
Orientation



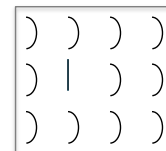
Shape



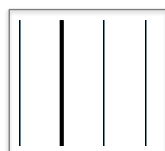
Line Length



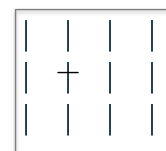
Curvature



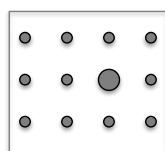
Line Width



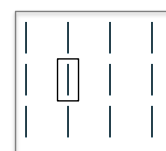
Added mark



Size

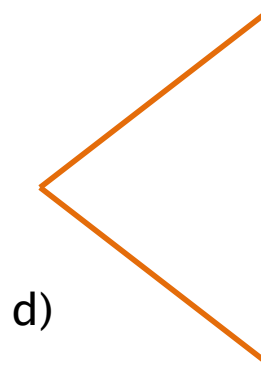
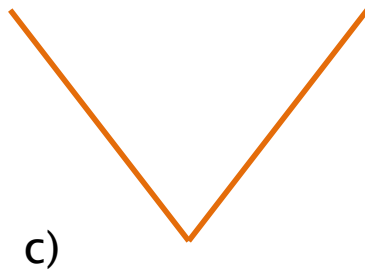
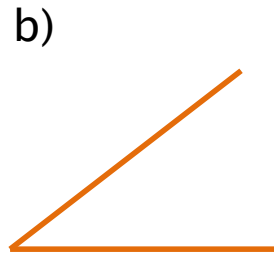
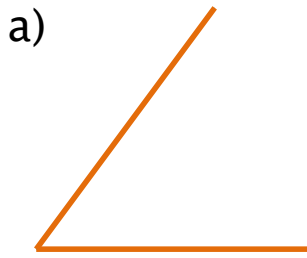


Enclosure



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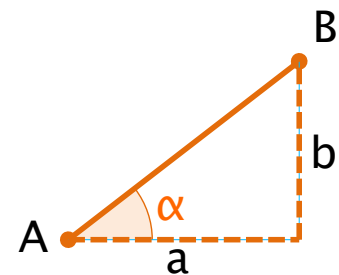
Orientation (angle or slope)



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Angle vs. Slope

- Slope of A-B is b/a
 - ♦ $\tan(\alpha)$
- Slope judgment typically falls back to an angle judgment
 - ♦ Given an error ϵ in the angle judgment
 - ♦ It is reflected in a slope error



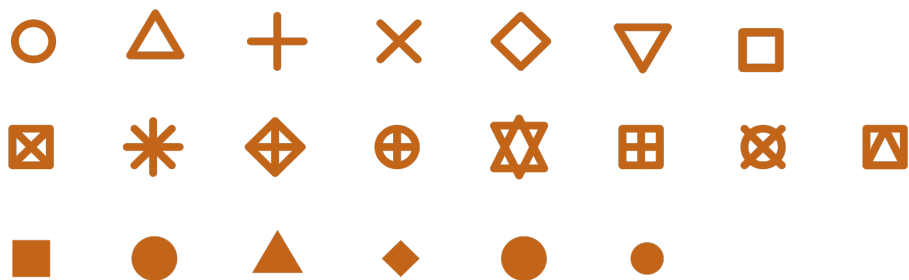
$$\tan(\alpha + \epsilon) - \tan(\alpha) = \epsilon \cdot \tan'(\alpha) = \frac{\epsilon}{\cos^2(\alpha)}$$

- Getting infinite as α approaches to $\pi/2$

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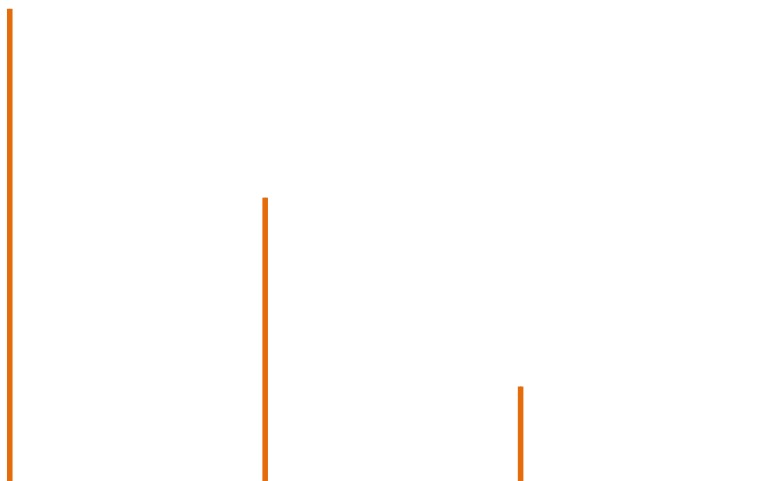
Shape

- There is no common quantitative semantics for the shapes
 - Unless they are characters...
 - ♦ Fill textures are shapes too



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Length



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Effect of context



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Curvature

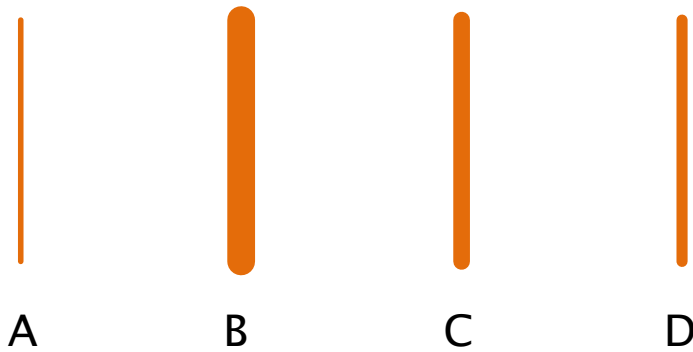
- There is no common magnitude assessment for the curvature



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Width

- Order can be identified
 - ◆ Difficult to appreciate actual magnitude



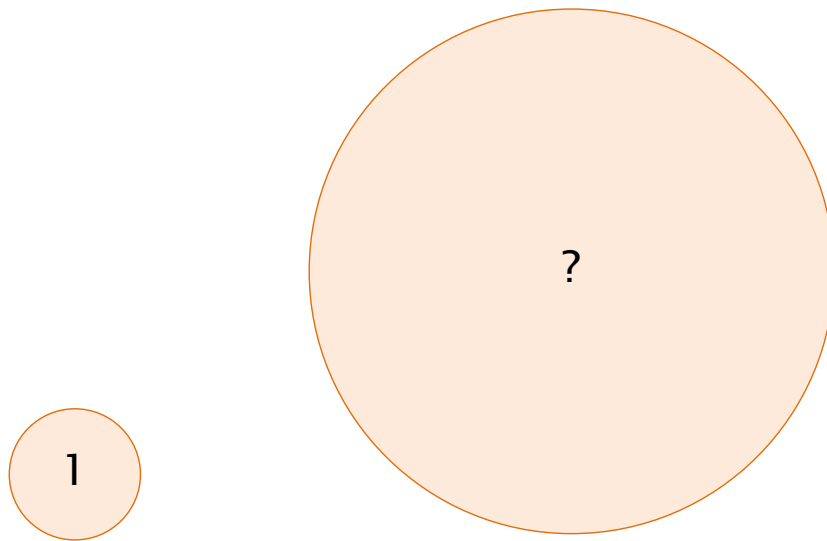
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Mark

- No common quantitative semantics of marks
- Number of marks could encode a natural number
 - ◆ Harder to read than a cipher

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Size / Area



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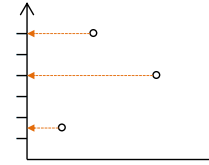
Enclosure

- No common quantitative semantics for enclosure
 - ♦ Except counting items enclosed

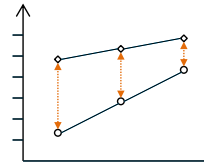
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Spatial Position

- Position along axis
 - ♦ Common scale
 - ♦ Distinct identical scales
 - Possibly un-aligned



- Distance



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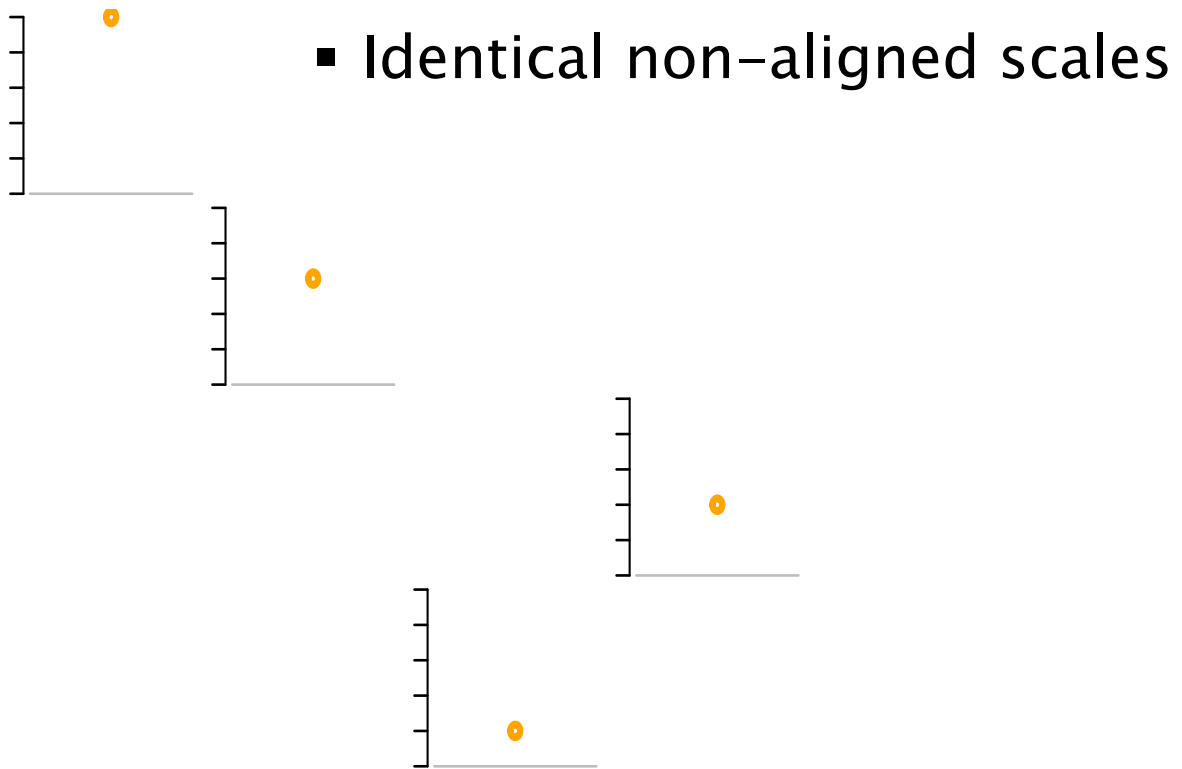
Position

- A common scale



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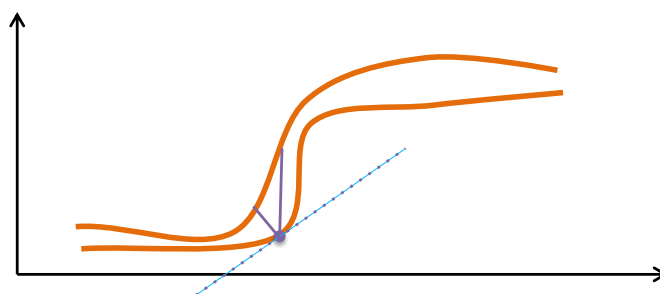
Position



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Distance

- Points
 - ♦ Use length of imaginary connecting lines
- Lines
 - ♦ Distance orthogonal to tangent
 - Not what is meant in xy plots



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Detection and Separation

Comparison is affected by:

- Detection
 - ◆ The capability to visually identify the objects that represent the data to be compared
- Separation
 - ◆ The distance between the objects to be compared
 - affects negatively the accuracy

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Attributes of color

- Hue 
- Saturation 
- Intensity
 - ◆ Luminance
 - ◆ Value

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Hue

- There is no common ordering semantics for hues
 - ♦ High spatial frequencies are perceived through intensity changes
 - ♦ Often perceived as separated into bands of almost constant hue, with sharp transitions between hues
- Nominal values can be represented by suitably spaced values



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Intensity

- ♦ a.k.a. Luminance, Value
- Provides a perceptually unambiguous ordering
 - ♦ Context can affect accuracy



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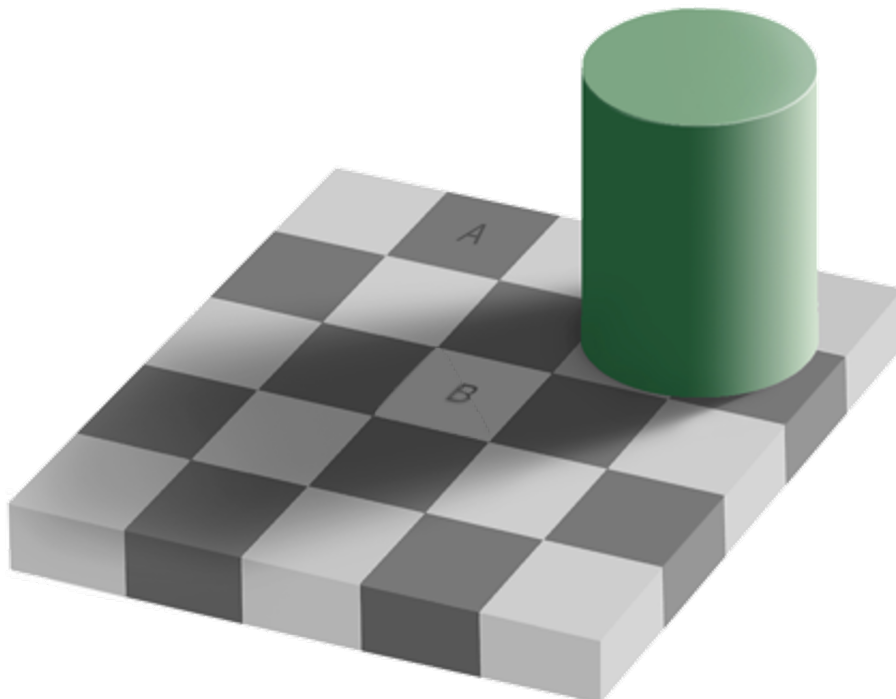
Saturation

- Perceptually difficult to associate an ordered semantics
 - ◆ Can be combined with hue to increase discrimination



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Effect of Context



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Effect of Context

- Use uniform background
 - ◆ To make distinct visual objects for the same feature look the same
- Use a background color that is contrasting enough with the visual objects' color
 - ◆ To make visual objects easily seen
- Avoid non-uniform background

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Color usage

- Ordinal measure should be mapped to increasing saturation **and** intensity
 - ◆ Avoid rainbow palette
- Use sequential or diverging palette
 - ◆ E.g.

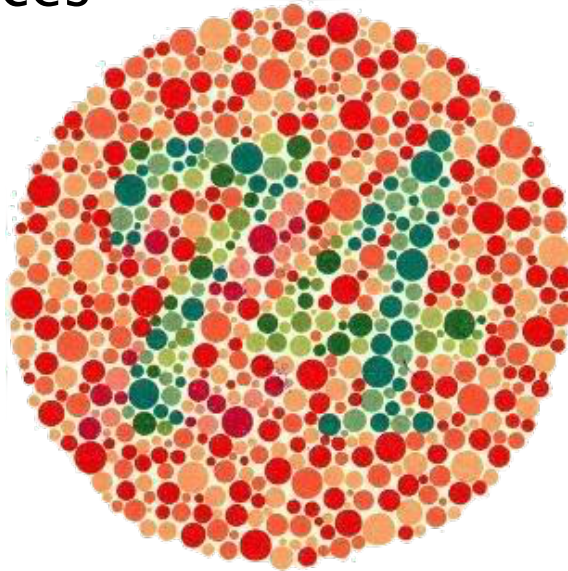


– <http://colorbrewer2.org/>

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Color Blindness

- Inability so see colors or perceive color differences



<http://www.color-blindness.com>

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Pre-Attentive attributes

Category	Attribute	Quantitative
Form	Orientation	Partly
	Length	Yes
	Line width	No
	Size	Partly
	Shape	No
	Curvature	No
	Added marks	No
	Enclosure	No
Color	Hue	No
	Intensity	Limited
Spatial position	2-D position	Yes
Motion	Flicker	No
	Direction	No

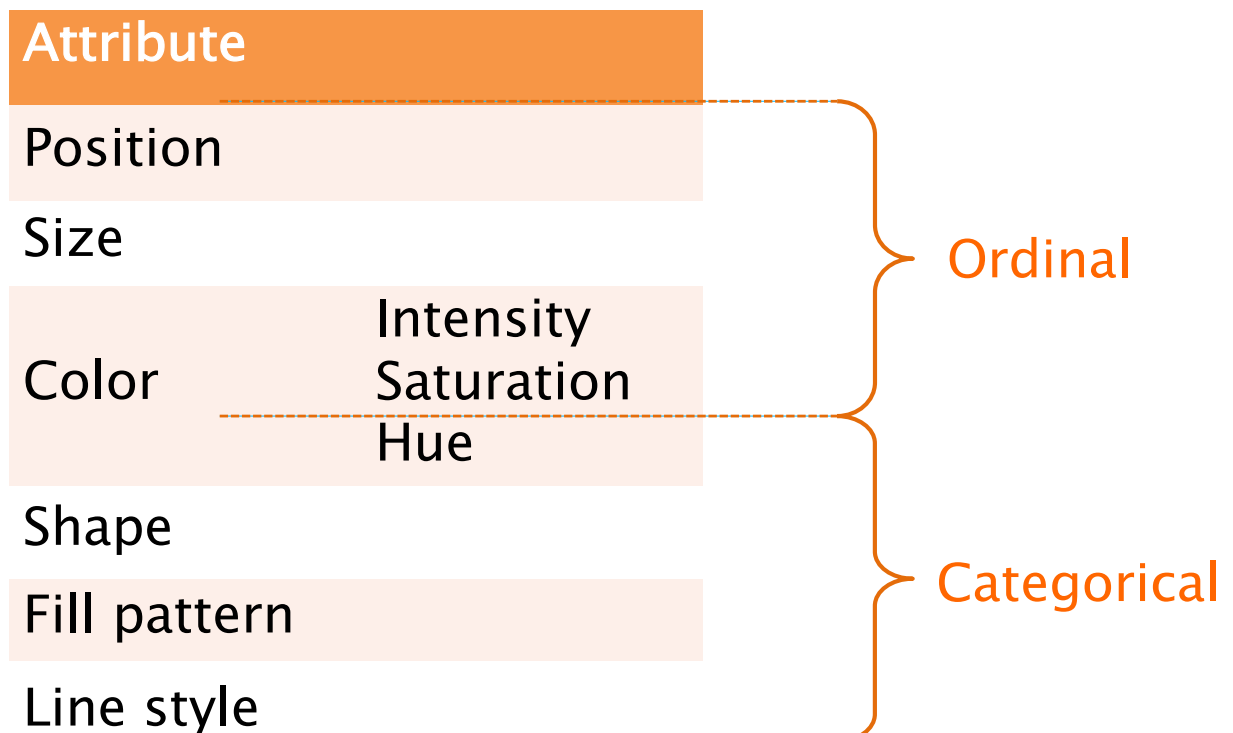
60

Visual Encoding: Quantitative

Object	Attribute
Point	Position (w.r.t. axis/axes)
Line	Length Position (w.r.t. axis/axes) Slope
Bar	Length
Shape	Size (area) Count

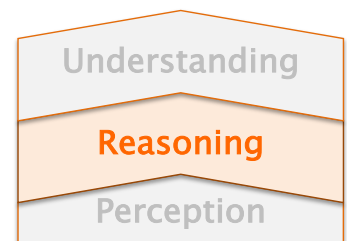
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Visual Encoding: Categorical



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VISUAL REASONING

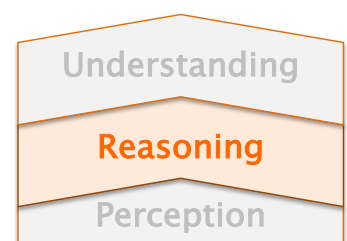


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Graph layout

Layout + visual attributes should allow:

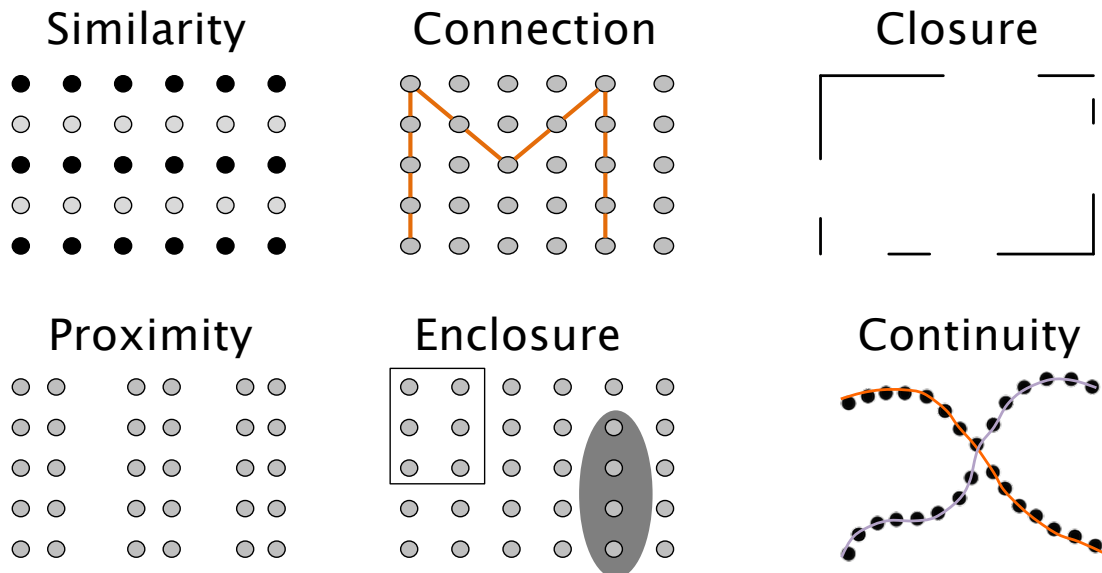
- **Discrimination**
 - ◆ Distinguish visual objects or group of –
- **Comparison**
 - ◆ Place visual objects in order
- **Magnitude assessment**
 - ◆ Evaluate the (relative) magnitude of visual objects



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Gestalt principles

- Visual features that lead the viewer to group visual objects together



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Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ Enclosure
 - ◆ Closure
 - ◆ Continuity
 - ◆ Connection

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Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate

- ◆ **Proximity**

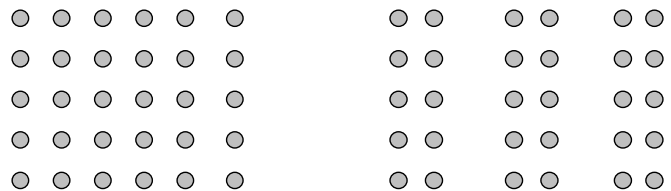
- ◆ Similarity

- ◆ Enclosure

- ◆ Closure

- ◆ Continuity

- ◆ Connection



Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate

- ◆ Proximity

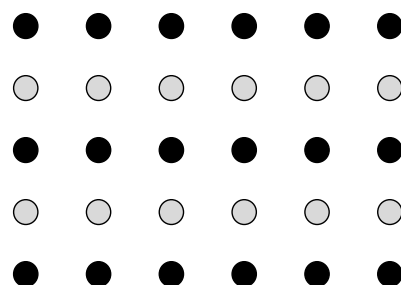
- ◆ **Similarity**

- ◆ Enclosure

- ◆ Closure

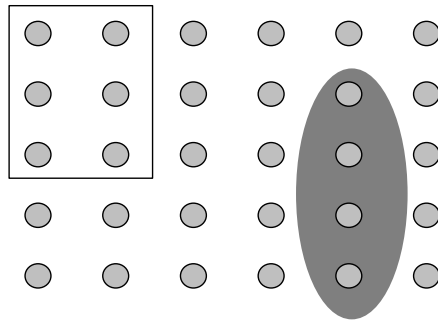
- ◆ Continuity

- ◆ Connection



Gestalt principles

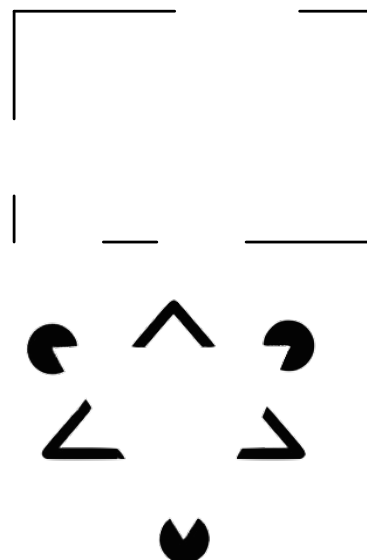
- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ **Enclosure**
 - ◆ Closure
 - ◆ Continuity
 - ◆ Connection



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Gestalt principles

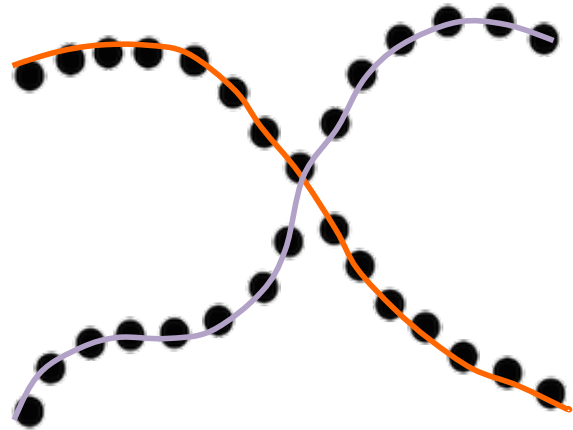
- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ Enclosure
 - ◆ **Closure**
 - ◆ Continuity
 - ◆ Connection



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Gestalt principles

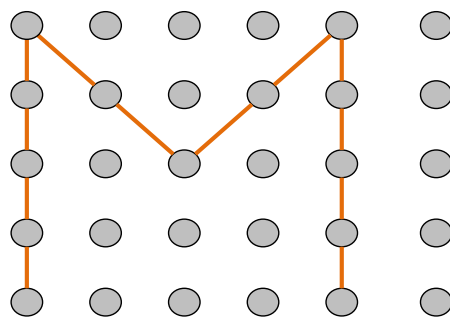
- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ Enclosure
 - ◆ Closure
 - ◆ **Continuity**
 - ◆ Connection



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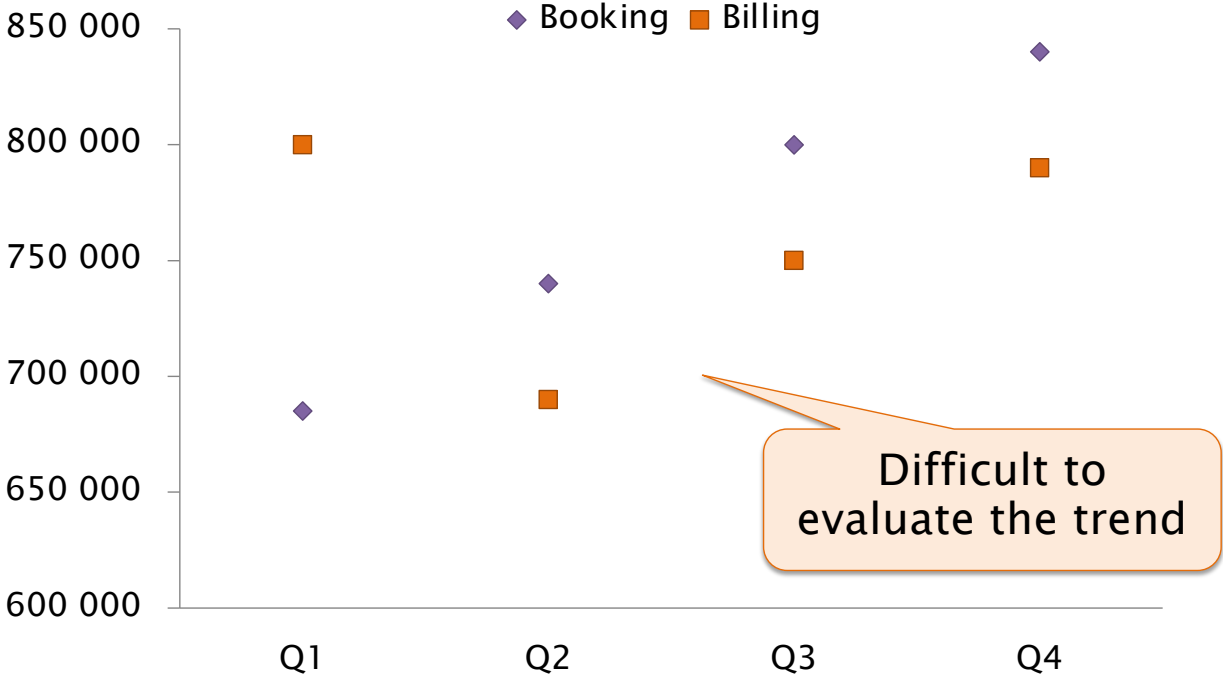
Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ Enclosure
 - ◆ Closure
 - ◆ Continuity
 - ◆ **Connection**

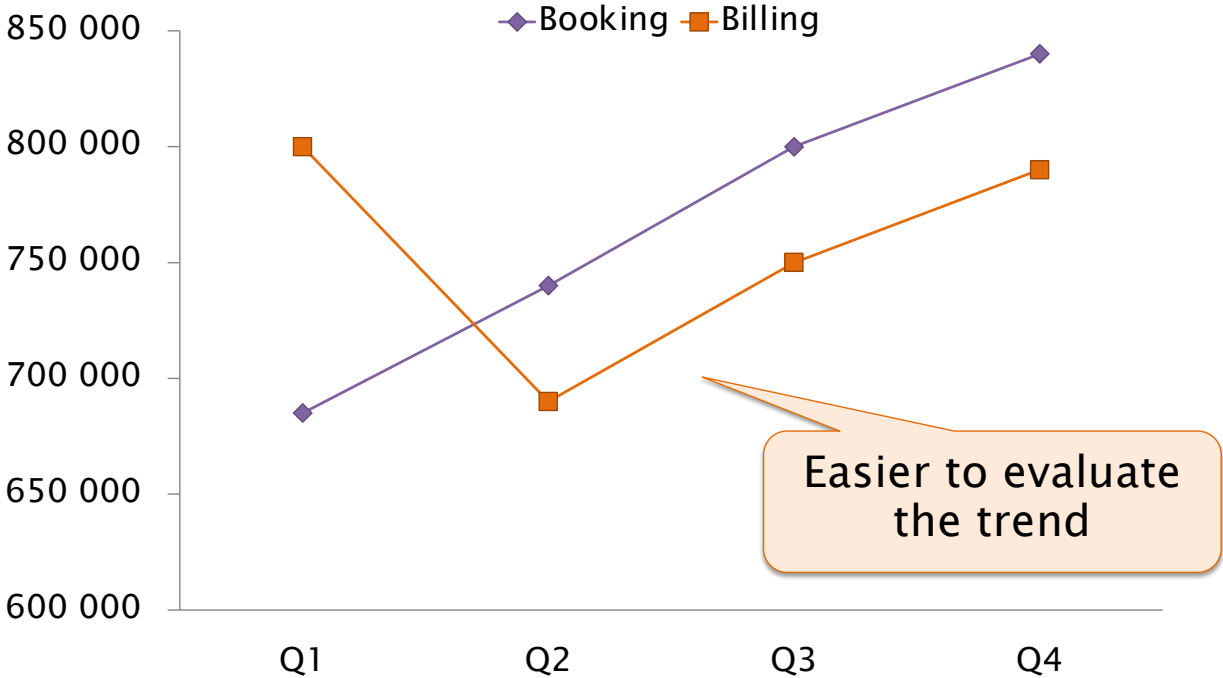


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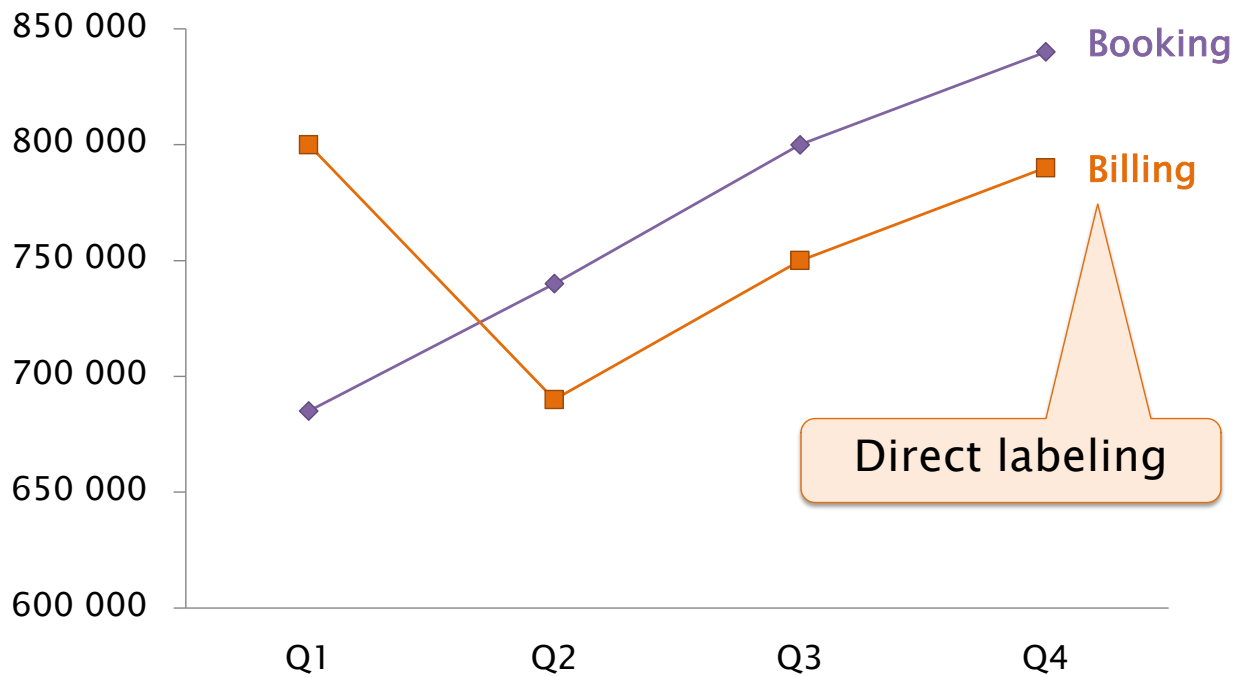
Similarity in Shape & Color



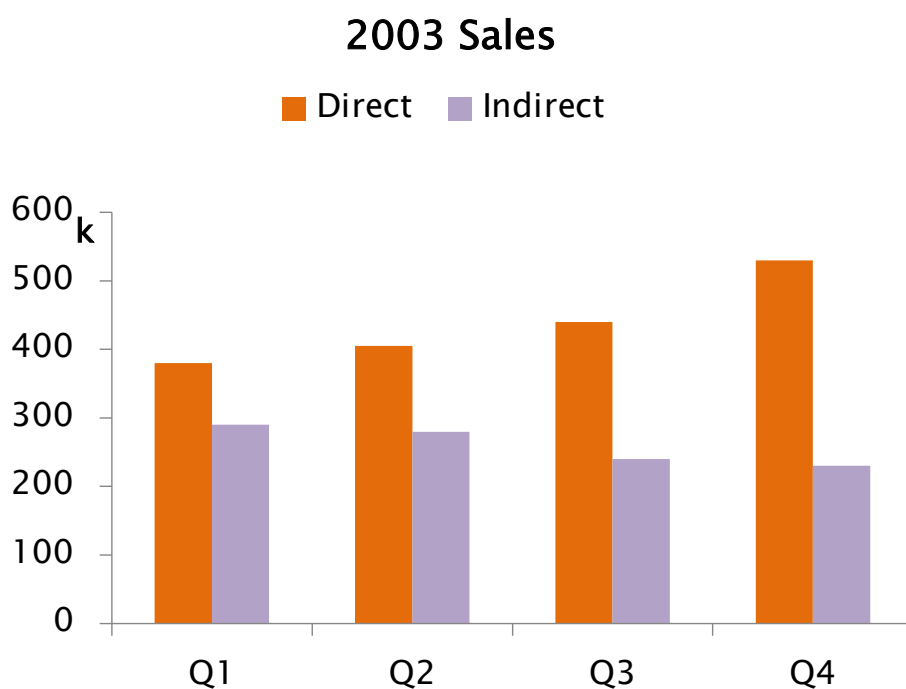
Similarity+Connection



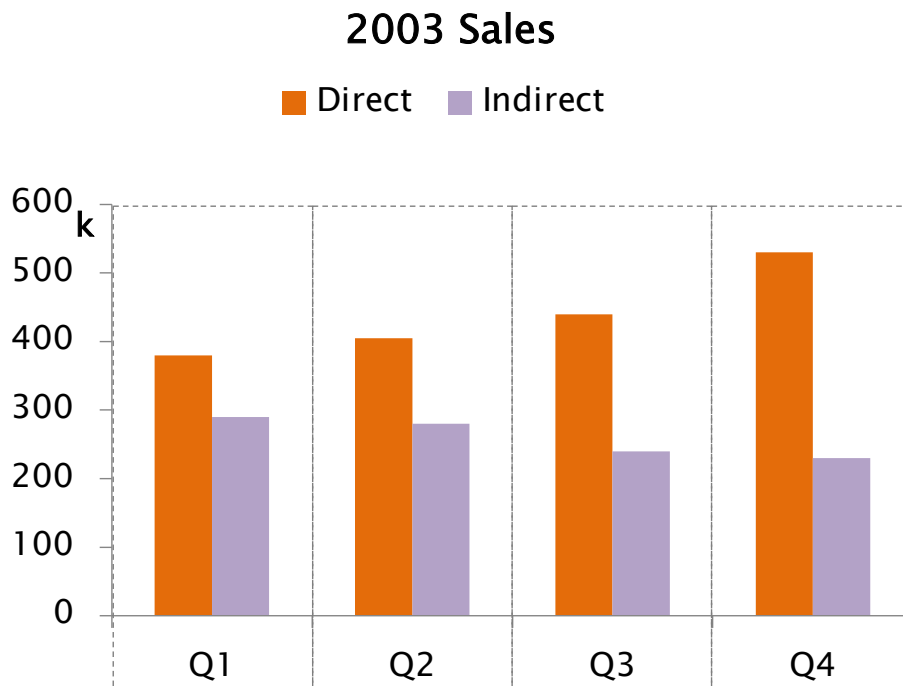
Similarity+Connection+Proximity



Similarity × Proximity

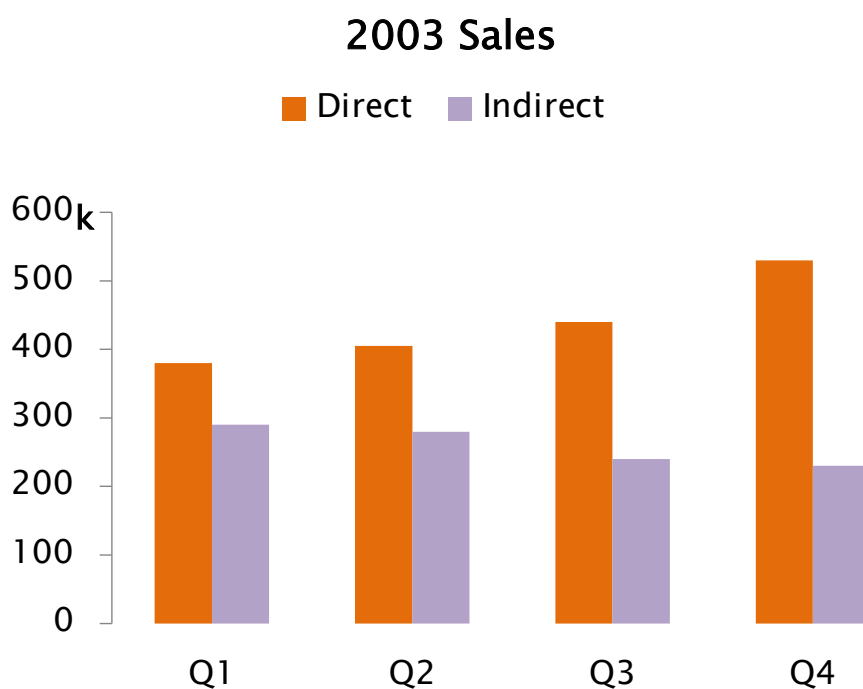


Similarity × Proximity & Enclosure



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Continuity replaces axis



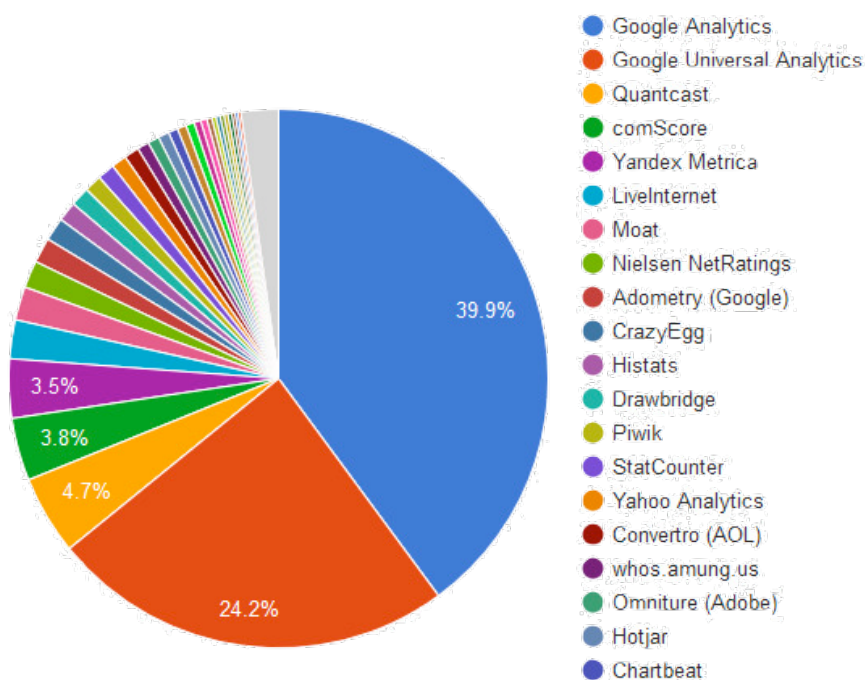
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Distinct perceptions

- The immediacy of any pre-attentive cue declines as the variety of alternative patterns increases
 - ♦ Even if all the distracting patterns are individually distinct from the target
 - ♦ For each single attribute no more than **four** distinct levels are immediately discernible
 - ♦ This limit affects the similarity principle

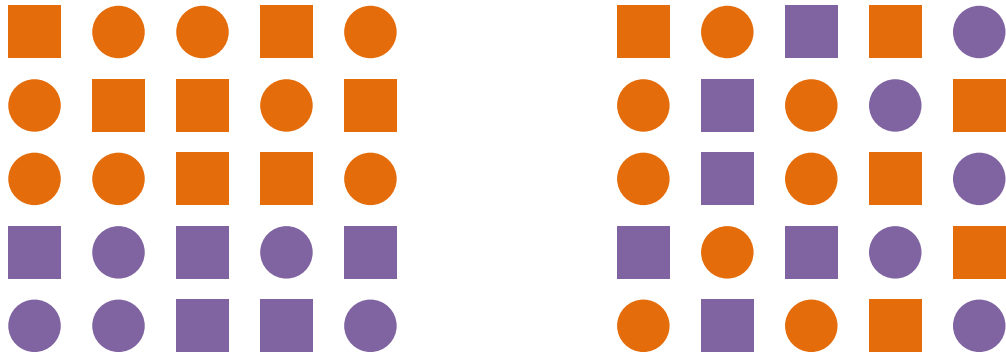
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Rainbow Pies



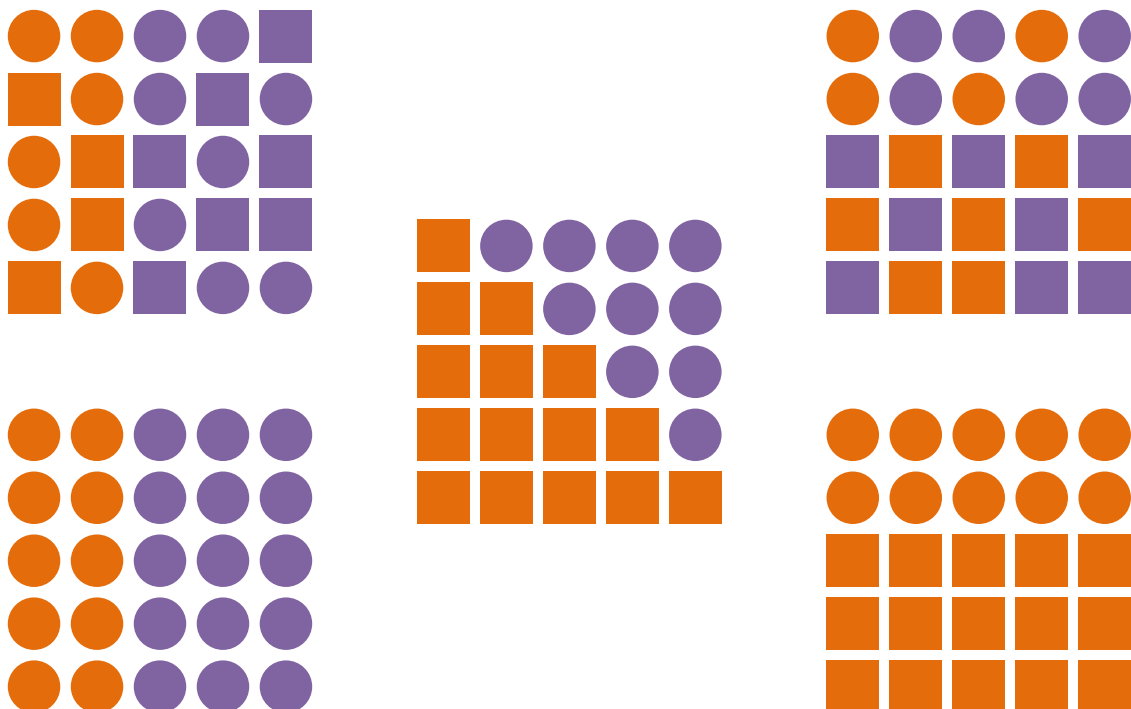
80

Attribute Interference



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Attribute Interference



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Cultural conventions

- Reading proceed from left to right and from top to bottom
 - ◆ At least in western culture
- What is at the top (on the left) precedes what is at the bottom (on the right) in terms of
 - ◆ Importance
 - ◆ Ordering
 - ◆ Time

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Emphasis

Attribute	Tables	Graphs
Line width	Boldface text	Thicker lines
Size	Bigger tables Larger fonts	Bigger graphs Wider bars Bigger symbols
Color intensity	Darker or brighter colors	
2-D position	Positioned at the top Positioned at the left Positioned in the center	

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VISUAL INTEGRITY

Principles of integrity

PUC

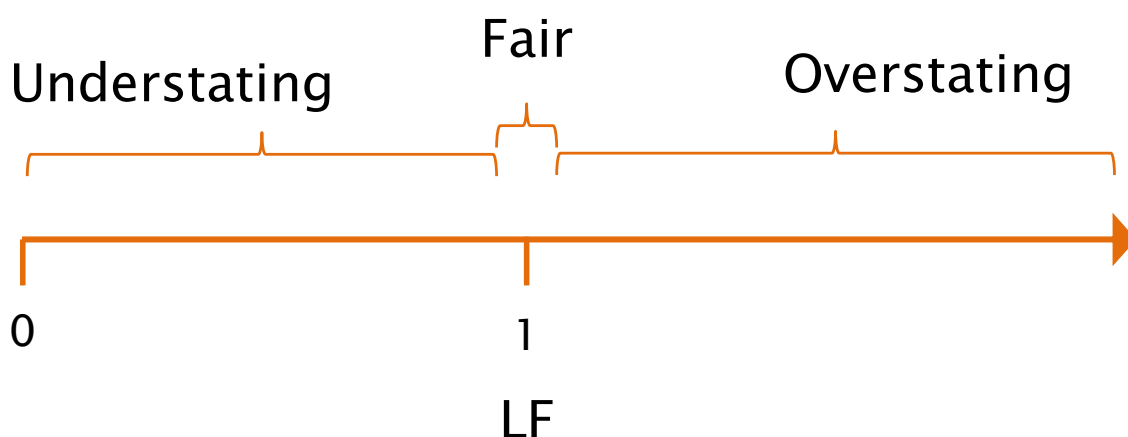
- **Proportionality**
 - ◆ Representation as physical quantities should be proportional to the represented numbers
- **Utility**
 - ◆ Graphical element should convey useful information
- **Clarity**
 - ◆ Labeling should counter graphical distortion and ambiguity

Proportionality

- The magnitude of visual attributes should represent faithfully the magnitude of measures
- They should allow
 - ♦ Discrimination: are they different?
 - ♦ Comparison: which is larger?
 - ♦ Magnitude Assessment: how much larger?

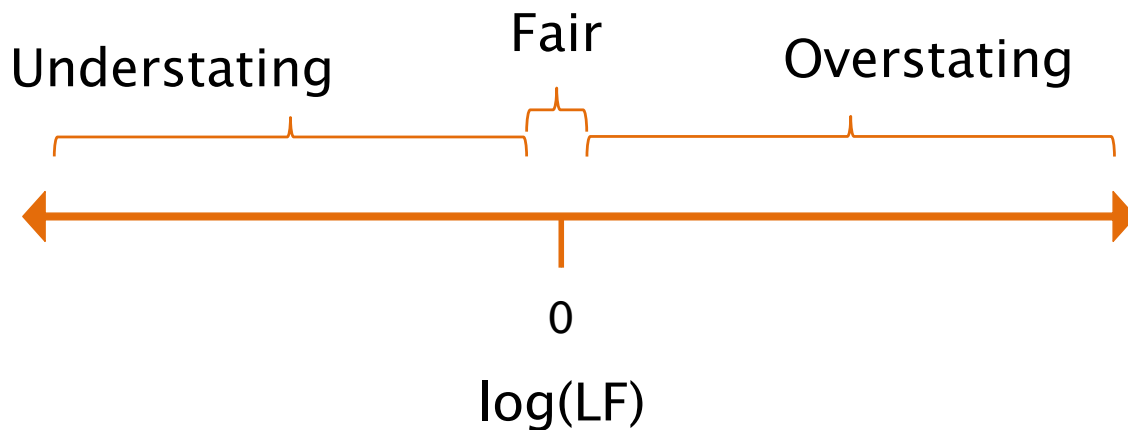
Lie Factor

$$LF = \frac{\text{size of effect shown in graphic}}{\text{size of effect in data}}$$



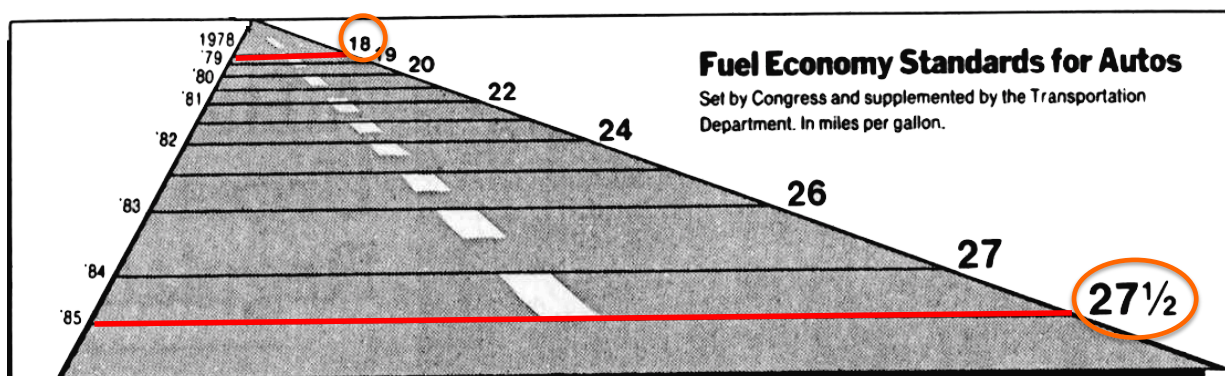
Lie Factor

$$LF = \frac{\text{size of effect shown in graphic}}{\text{size of effect in data}}$$



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Lie Factor – Example



$$\frac{18.7}{2.2} = 8.5 \text{ on graphic}$$

$$\frac{27.5}{18} = 1.52 \text{ in data}$$

$$LF = 8.5 / 1.52 = 5.59$$

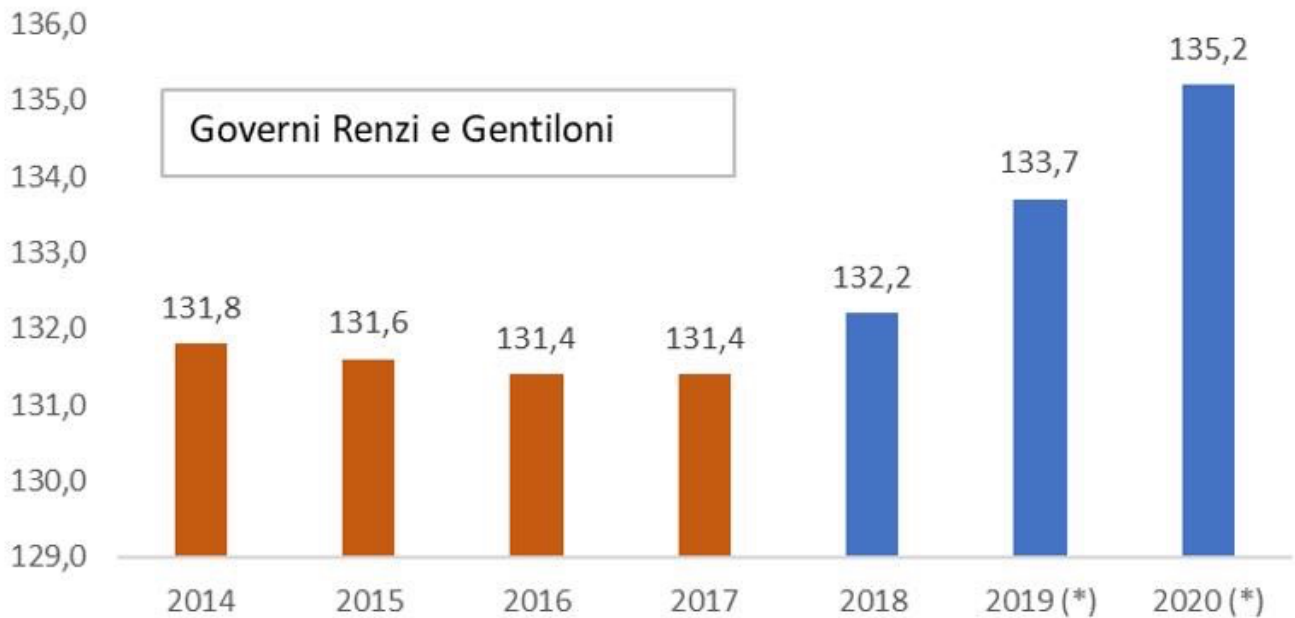
90

Lie Factor – Example

Debito pubblico (% PIL)

(*) previsioni Commissione UE

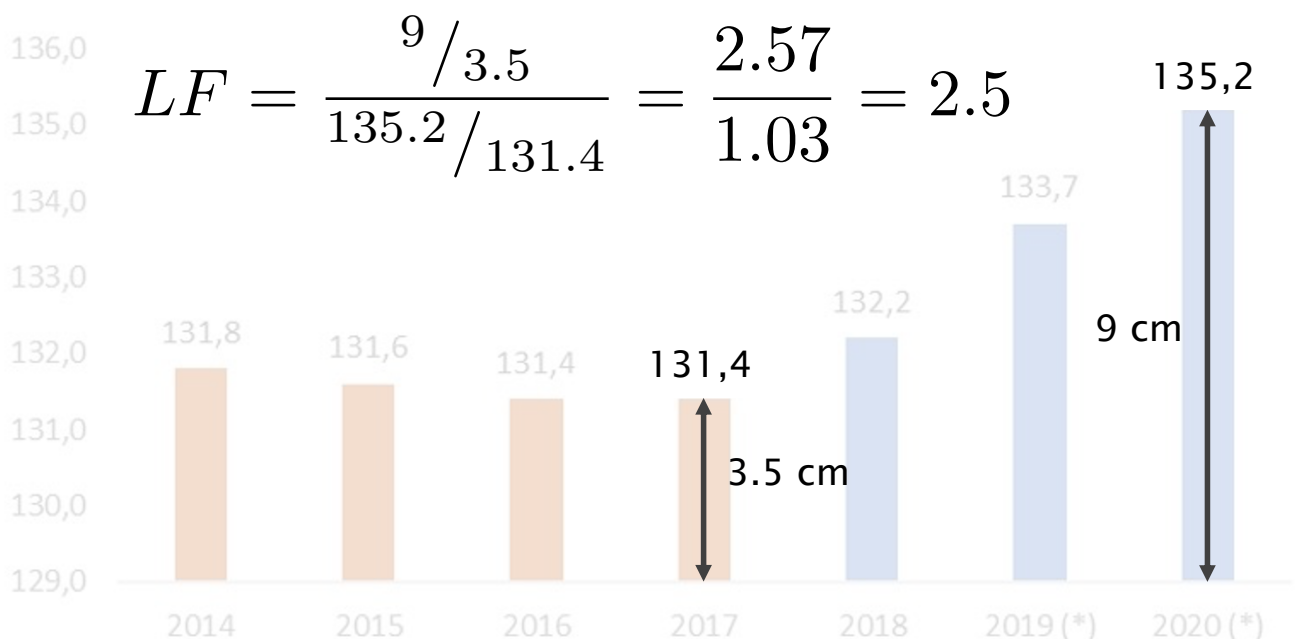
Governo Conte



Lie Factor – Example

Debito pubblico (% PIL)

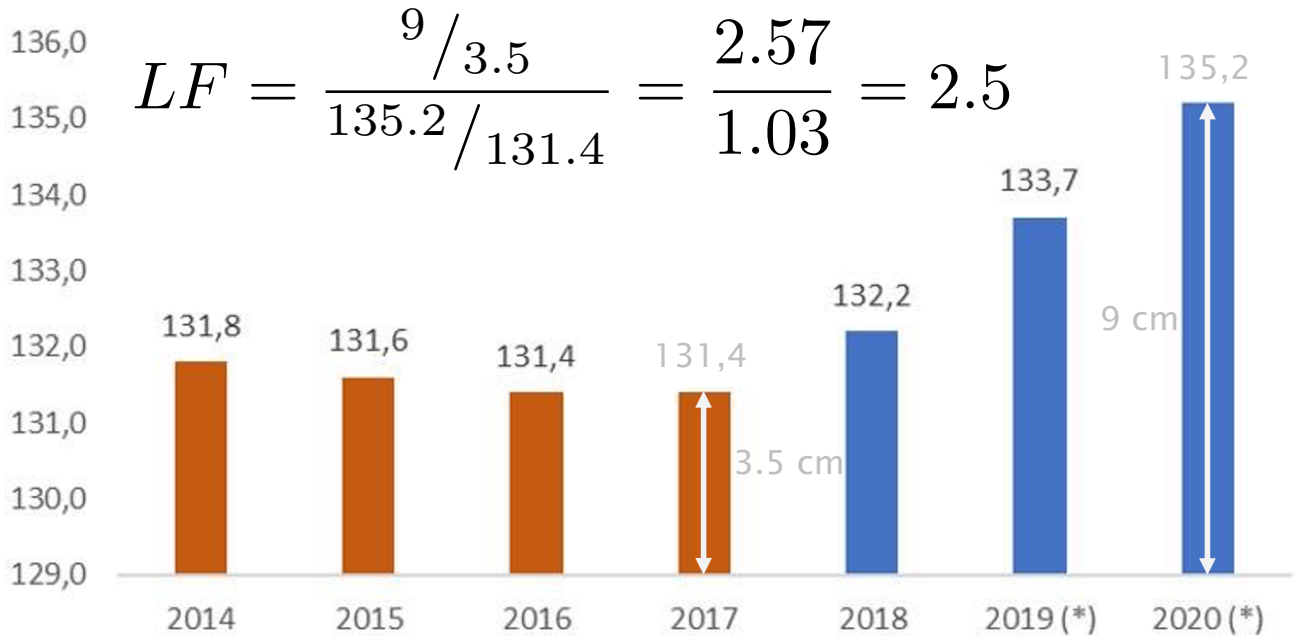
(*) previsioni Commissione UE



Lie Factor – Example

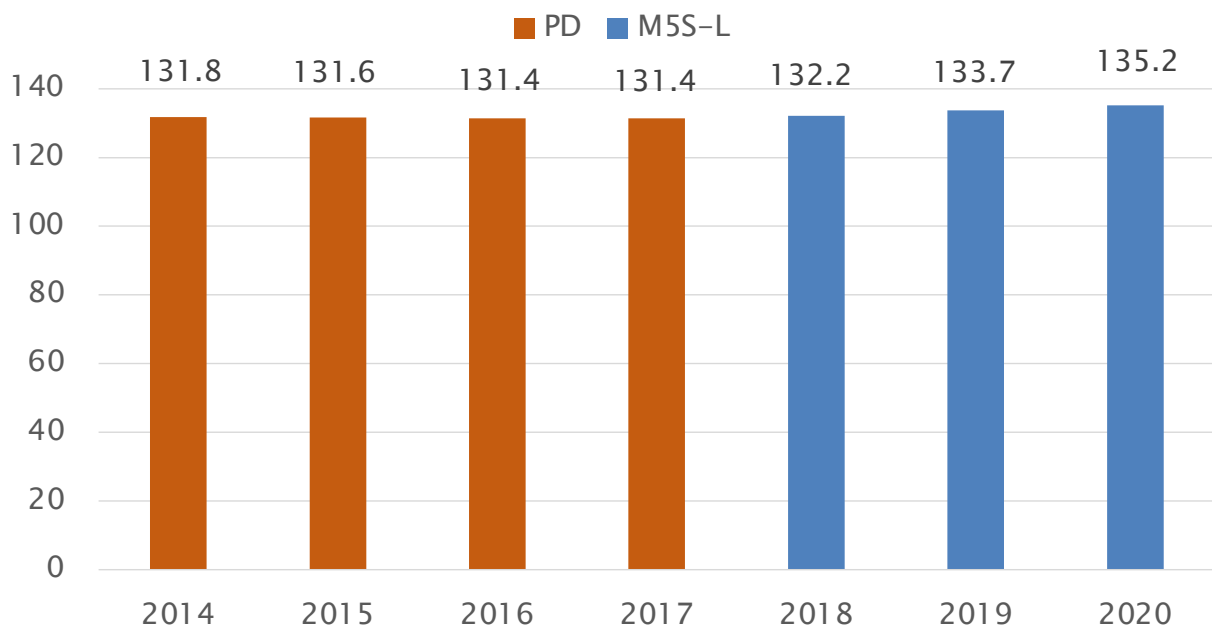
Debito pubblico (% PIL)

(*) previsioni Commissione UE

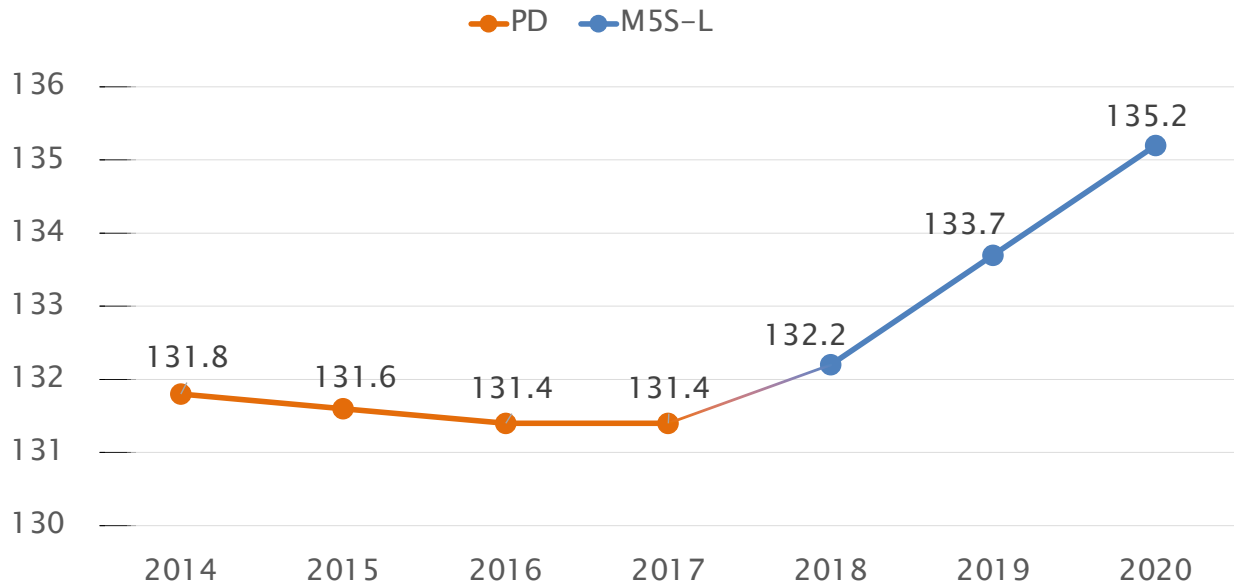


Lie Factor – Redesign

Debito Pubblico (% PIL)



Debito Pubblico (% PIL)



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Guidelines for design

- Keep the physical Lie Factor = 1
- Limit the perceptual Lie Factor as much as possible
 - ♦ Per Steven's law, avoid area comparisons

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- Every element should convey useful information
- Unnecessary visual objects or attributes distract from the message
 - ◆ Different attributes trigger a search for a rationale (e.g. random colors)

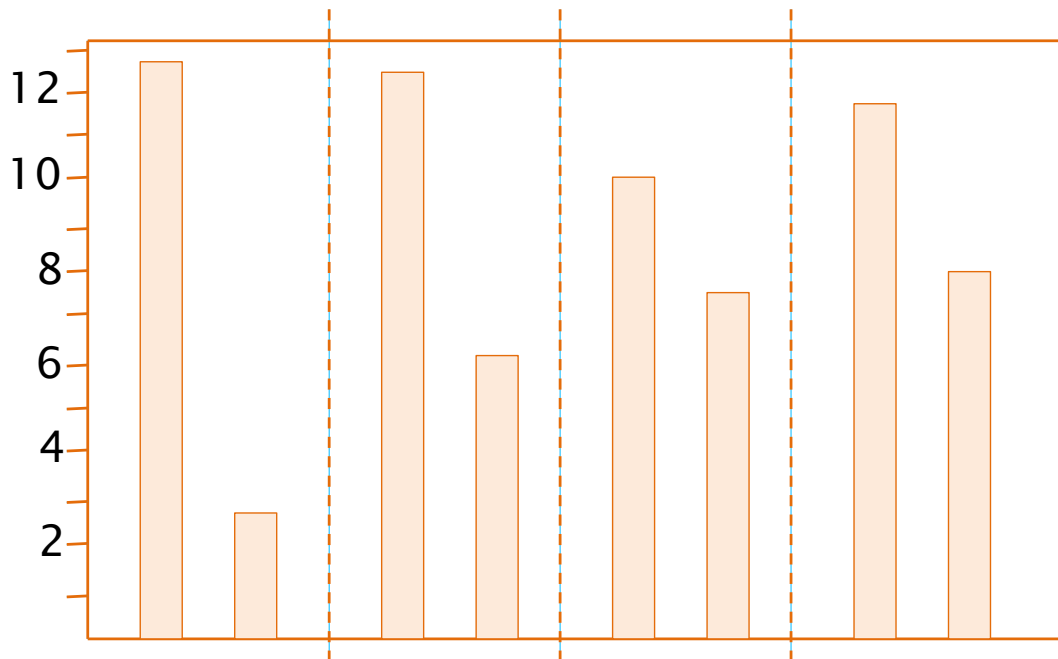
Data-ink ratio = $\frac{\text{data ink}}{\text{total ink used to print the graphic}}$

- Proportion of a graphic's ink devoted to the non-redundant display of data information

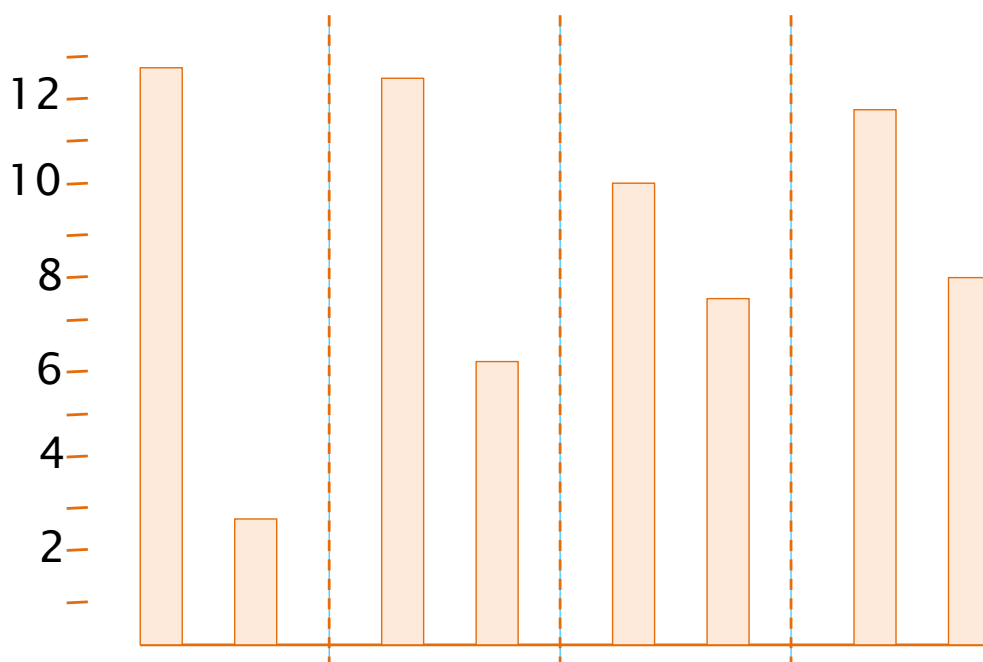
- ◆ Or:

$$1 - \frac{\text{ink that can be erased without loss of information}}{\text{total ink used to print the graphic}}$$

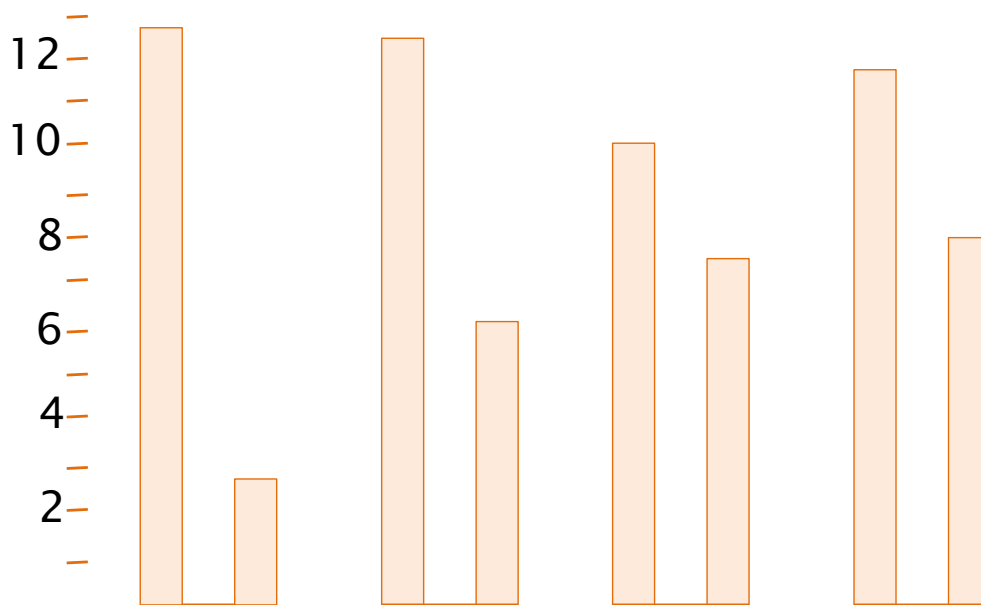
Data-ink



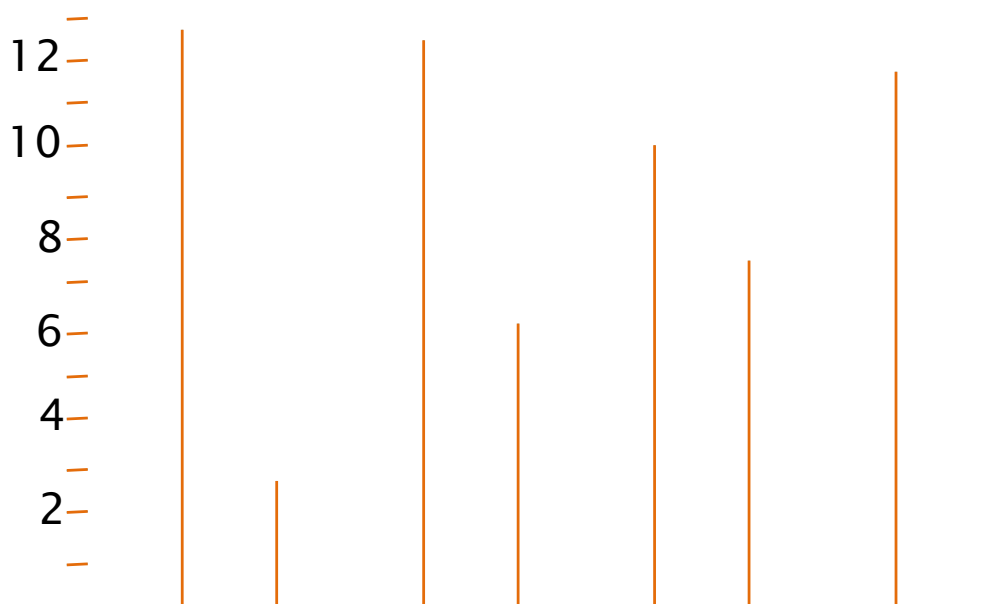
Data-ink



Data-ink



Data-ink



Tufte's proposed redesign

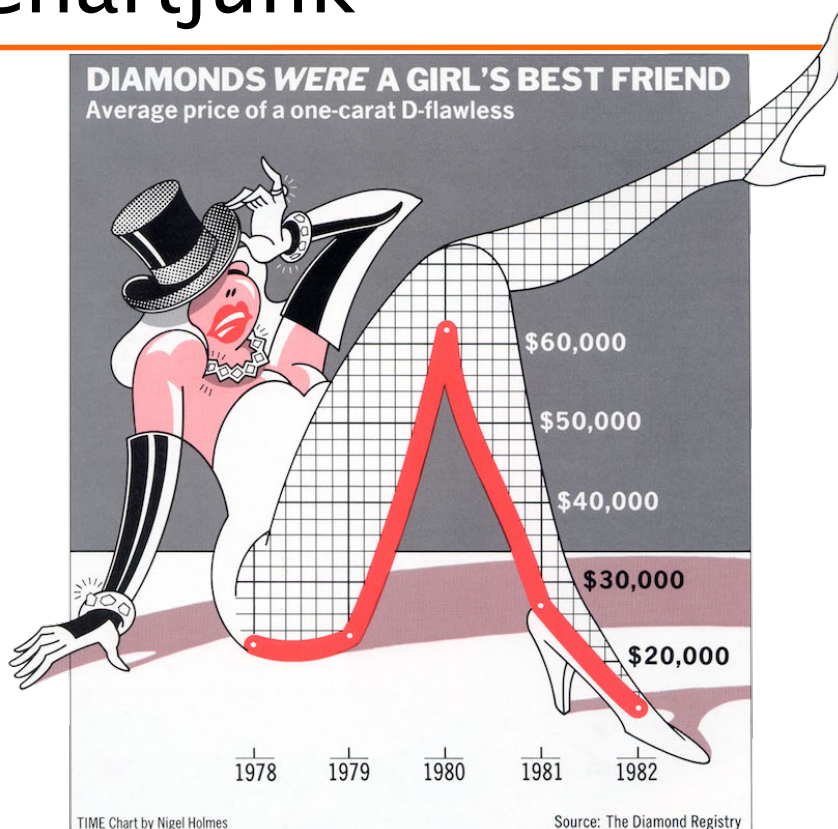
- Maximize data-ink ratio
 - ◆ Erase non-data-ink
 - ◆ Erase redundant data-ink
- “Within reason”

Above all else show the data
E. Tufte

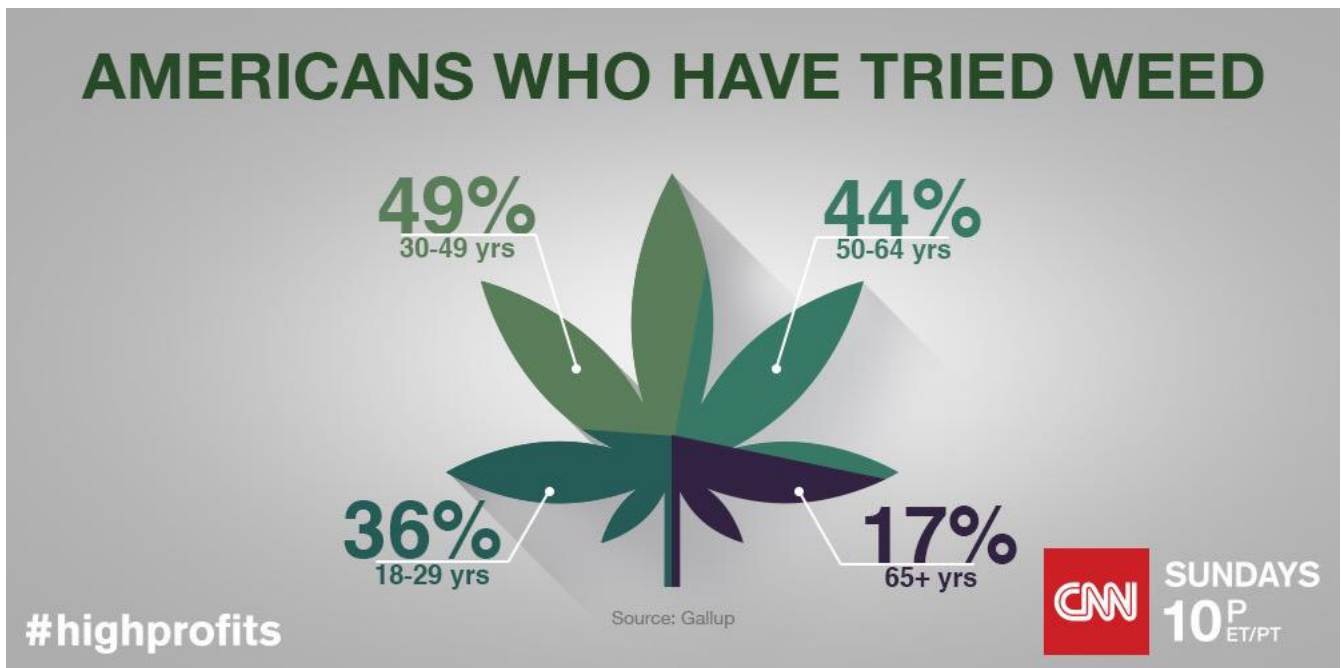
Use of contrast

- Include differences corresponding to actual differences
- Effective when one item is different in a context of other items that are the same
 - ◆ Bright saturated color among mid colors

- The presence of unnecessary elements that distract or hide the message conveyed by the diagram



Nigel Holmes:
<http://nigelholmes.com>



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Clarity

- Visual encoding and layout should make perception tasks easy and effortless
- Textual and support elements should provide effective support to understanding the information
- Any variation in the graph should represent useful information otherwise it is noise obfuscating the message

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- **Textual** elements should provide effective support to understanding
 - ◆ Hierarchical
 - Size and position reflects importance
 - ◆ Readable
 - Large enough
 - ◆ Horizontal
 - ◆ Close to data (avoid legends)
- Always label the axes

- Get it right in black and white
- Use medium hues or pastels
 - ◆ Bright colors distract and tire out
- Use color only when needed to serve a particular communication goal

Cognitive Dissonance



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Detection and Separation



Efficiency and efficacy of perception tasks is affected by:

- **Detection**

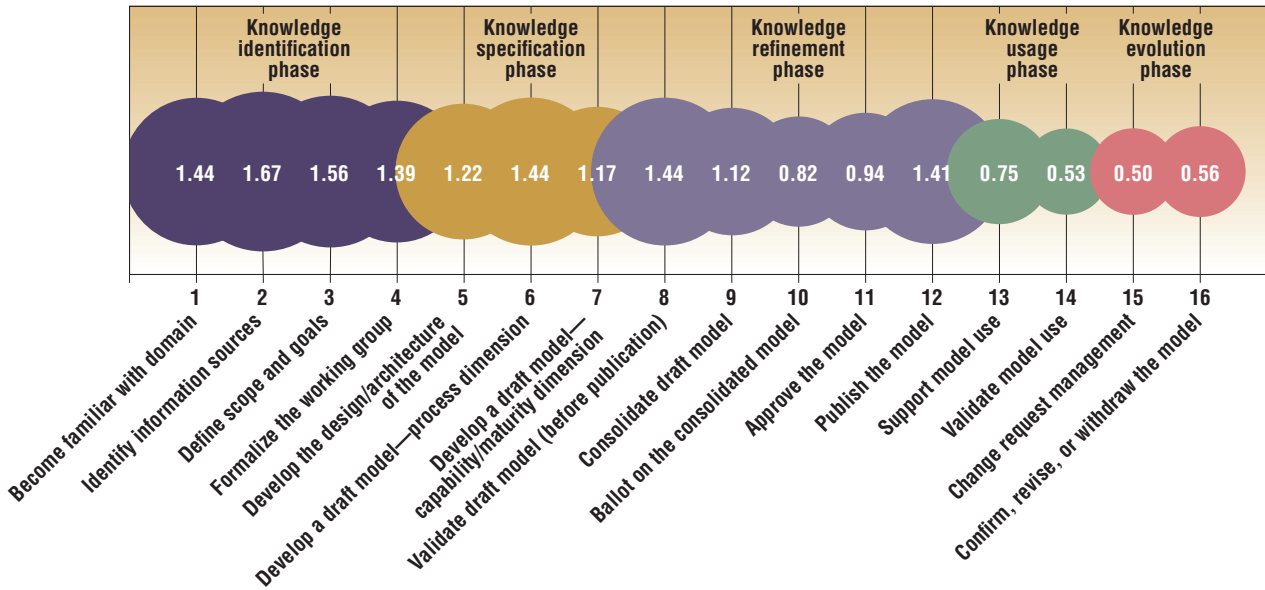
The capability to visually identify the objects that represent the data to be compared

- **Separation**

The distance between the objects to be compared

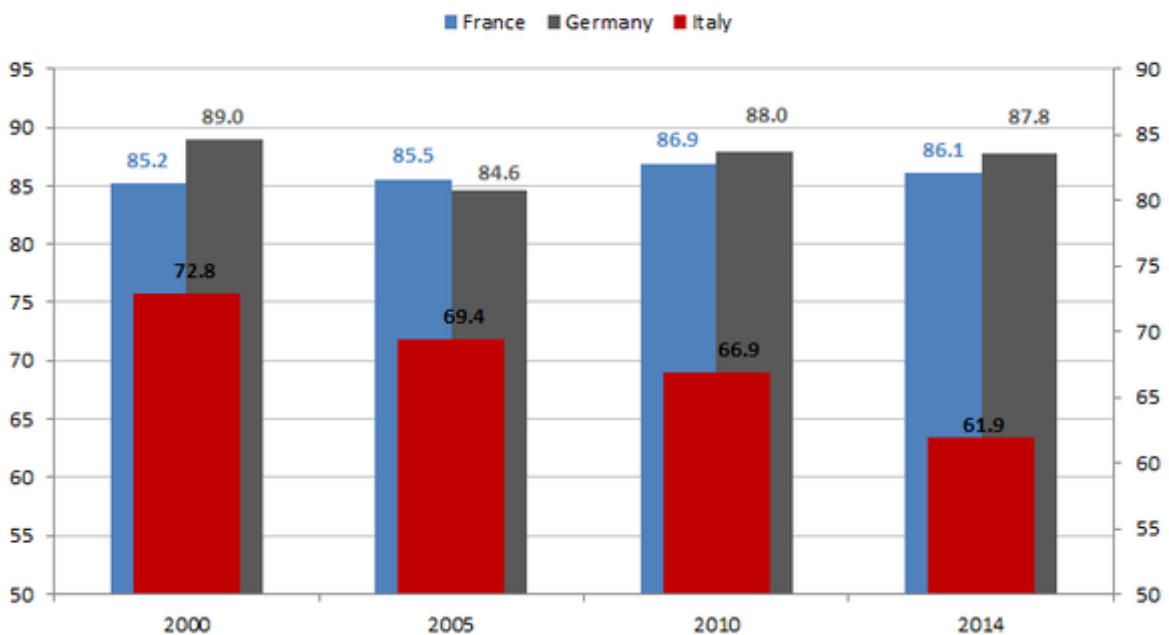
– affects negatively the accuracy

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Example

Trends in employment rates of 25-34 with a tertiary degree



Analysis

- Proportionality
 - ◆ Due to non-zero base bars, it has a large lie factor (2.2):
 - ratio of real values: 87.8 : 61.9
 - ratio on graph: 37.8 : 11.9
- Utility
 - ◆ Most elements appear useful
 - ◆ X-axis ticks can be removed
 - ◆ Y grid could be made less prominent

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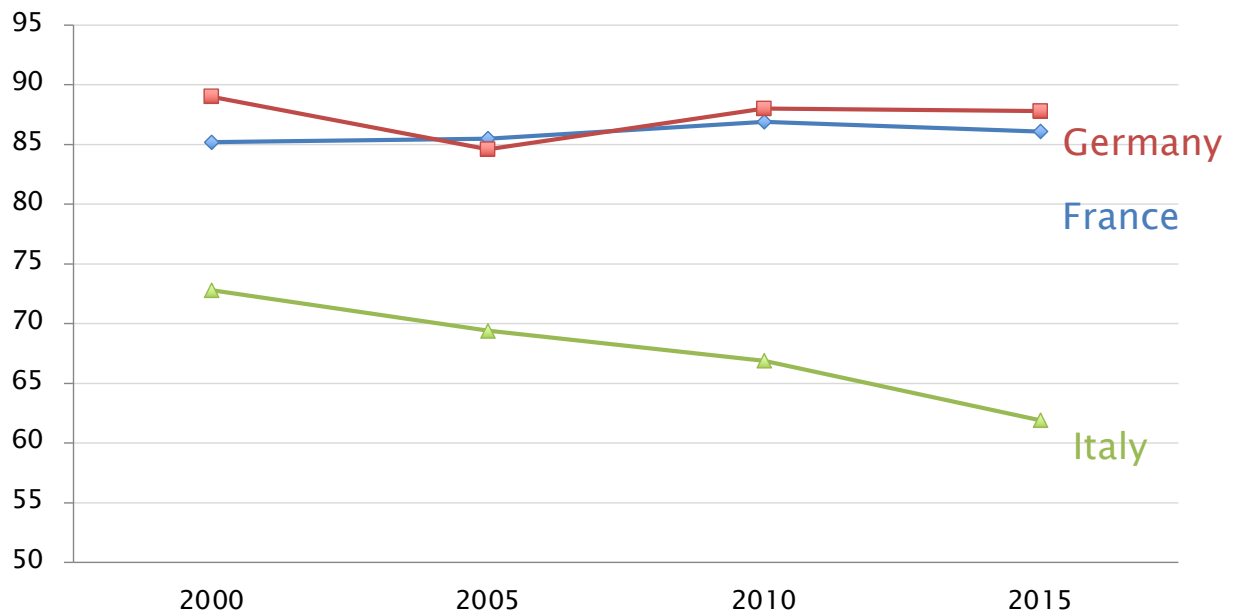
Analysis

- Clarity
 - ◆ It uses a **dual scale** that confuses and makes very hard a visual comparison of the values and further distorting the compared values.
 - ◆ The dual scale is not mentioned anywhere and it is not clear which values refer to which scale.
 - ◆ In general the usage of bars is not the most appropriate visual representation if the goal is to show a trend or evolution in time.

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Redesign

Trends in employment rates of 25–34 with a tertiary degree



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- I. Inbar, N. Tractinsky and J. Meyer. Minimalism in information visualization: attitudes towards maximizing the data–ink ratio.
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 - ♦ http://www.perceptualedge.com/articles/visual_business_intelligence/rules_for_using_color.pdf
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 - ♦ http://ieeexplore.ieee.org/xpls/abs_all.jsp?arnumber=4118486
- <http://www.color-blindness.com>
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